

WORKSHOP ON PHARMACOKINETICS-PHARMACODYNAMICS OF ANTICANCER DRUGS: RESISTANCES AND SYNERGIES, PARIS, DECEMBER 18-19, 2008

Towards optimisation of cancer chronotherapeutics by taking into account patient-specific constraints: Mathematical models for individualised medicine

> Jean Clairambault BANG project-team, INRIA Paris-Rocquencourt & INSERM U 776, Villejuif

http://www-c.inria.fr/bang/JC/Jean\_Clairambault\_en.html

## Outline of the talk

1. Modelling (circadian) pharmacokinetics-pharmacodynamics (PK-PD) ...at the molecular level in blood and in tissues

2. Modelling cell proliferation and its control mechanisms ...at the level of cell populations in tissues

3. Modelling the circadian system and its disruptions ...at both the central and peripheral levels

4. Optimising chronotherapeutics: objectives and constraints

5. Individualising treatments: identifying patient-specific parameters

1. Action of classical cytotoxic drugs: (5FU, Oxaliplatin, Irinotecan) Pharmacokinetic-pharmacodynamic (PK-PD) modelling

Ordinary differential equations (ODEs)

#### Molecular PK-PD modelling in oncology

"Pharmacokinetics is what the organism does to the drug, Pharmacodynamics is what the drug does to the organism"

- *Input*: an intravenous [multi-]drug infusion flow
- Drug concentrations in blood *and tissue* compartments (PK)
- Control of targets on the cell cycle *in tissues* (cell population PD)
- *Output*: a resulting growth rate in tumour and healthy tissues
- *Optimisation* = decreasing proliferation in tumour tissues while maintaining normal proliferation in healthy tissues

## Example: 5FU (with drug resistance) + Leucovorin

P = Plasma [5FU]

F = Intracellular [FdUMP]

Q = Plasma [LV]

L = Intracellular [LV]

N = [nrf2] efflux Nuclear Factor

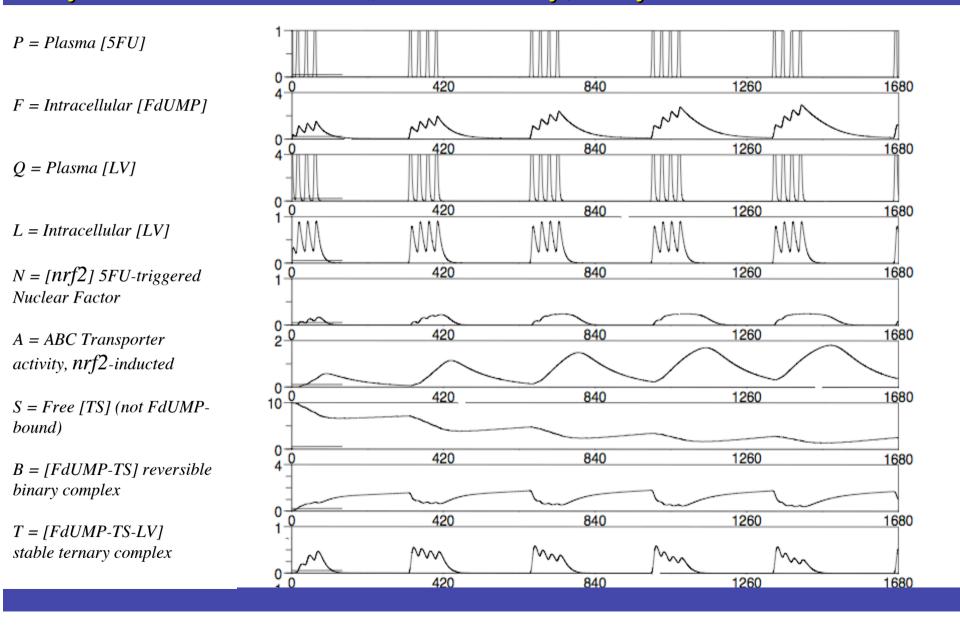
A = ABC Transporter activity

- *S* = *Free* [*TS*] (*not FdUMP-bound*)
- B = [FdUMP-TS] binary complex
- T = [FdUMP-TS-LV] irreversible ternary complex

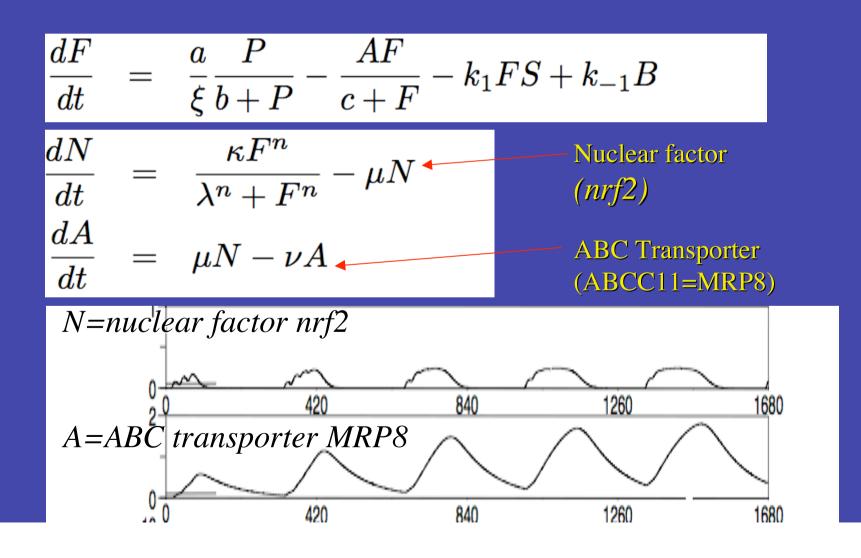
where  $l_{DPD} = l_{DPD\_BASE} \left\{ 1 + \varepsilon \cos \frac{2\pi i}{2\pi i} \right\}$ 

$$\frac{dP}{dt} = -k_0P - \frac{aP}{b+P} - l_{DPD}\frac{P}{m_{DPD}+P} + \begin{pmatrix} i(t) \\ W \\ \frac{dF}{dt} \\ = \frac{a}{\xi}\frac{P}{b+P} - \frac{AF}{c+F} - k_1FS + k_{-1}B \\ \frac{dQ}{dt} \\ = -k_2Q + \frac{j(t)}{V} \\ \frac{dL}{dt} \\ = \frac{k_2}{\xi}Q - k_3L - k_4BL \\ \frac{dN}{dt} \\ = \frac{\kappa F^n}{\lambda^n + F^n} - \mu N$$
Input = 5FU infusion flow
$$\frac{dA}{dt} \\ = -k_1FS + k_{-1}B + \theta_{TS}(S_0 - S) \\ \frac{dB}{dt} \\ = k_1FS - k_{-1}B - k_4BL \\ \frac{dT}{dt} \\ = k_4BL - v_T T$$
Output = blocked Thymidylate Synthase
$$\frac{t - \varphi_{DPD}}{24} \\ \right\} \quad \text{and} \quad S_0 = S_{0\_BASE} \left\{ 1 + \delta \cos \frac{2\pi(t - \varphi_{TS})}{24} \right\}$$

# Simulation: 5 courses of 2 week-therapy courses $i(t)=i_0[1+\sin\{2\pi(t-\varphi_{5FU}+9)/12\}]$ and $j(t)=j_0[1+\sin\{2\pi(t-\varphi_{LV}+9)/12\}]$ , then zero for 12 hours 4 days of 4FU+LV infusion, 12 hours a day, every other week

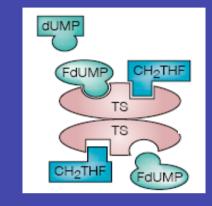


Induction of ABC Transporter activity by FdUMP-triggered synthesis of nuclear factor *nrf2* 



# Targeting Thimidylate Synthase (*TS*) by FdUMP: Formation of binary and ternary *TS*-complexes

$$\begin{aligned} \frac{dS}{dt} &= -k_1 F S + k_{-1} B + \theta_{TS} (S_0 - S) \\ \frac{dB}{dt} &= k_1 F S - k_{-1} B - k_4 B L \\ \frac{dT}{dt} &= k_4 B L - v_T T \end{aligned}$$



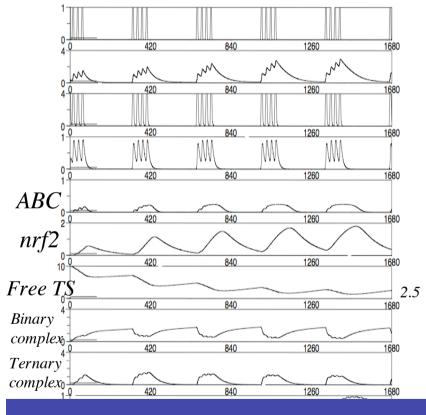
B-L = T (FdUMP-TS-LV 3-complex)B + LS=free TS 420 840 1260 1680 *B=binary* complex 420 840 1260 1680 *T=ternary*  $\sim$  $\sim$  $\sim$ complex 420 840 1260 1680

 $F + S \longrightarrow F - S = B (FdUMP - TS 2 - complex)$ 

#### Examples of features of the model:

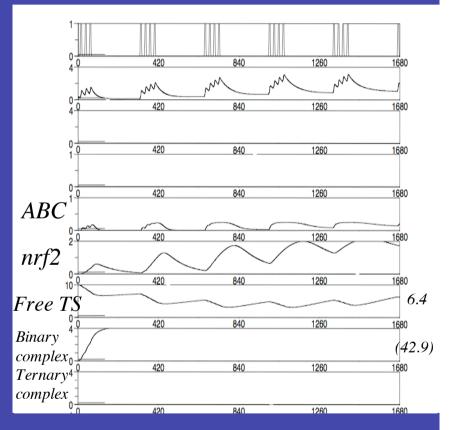
a) 5FU with/without LV in cancer cells (=ABC transporter MRP8+)

With Leucovorin added in treatment



Free TS decays to zero = cancer cells die

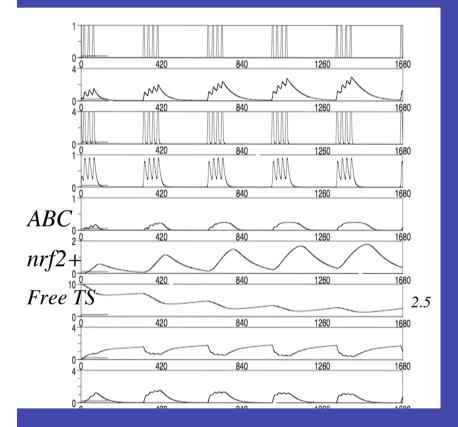
Without Leucovorin added



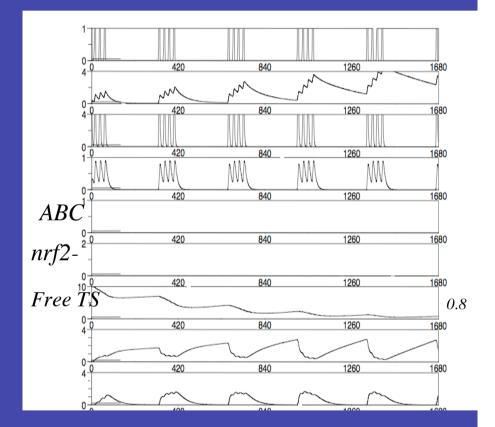
Free TS maintains its level = cancer cells survive

#### b) 5FU+LV with/without MRP8 (cancer vs. healthy cells)

#### Cancer cells (ABC+=MRP8+)

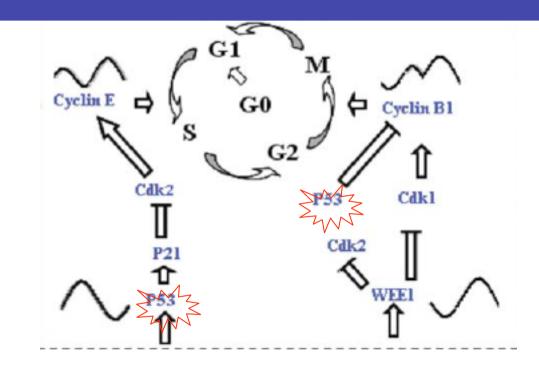


#### Healthy cells (ABC-=MRP8-)



Cancer cells resist more than healthy cells, due to lesser exposure to FdUMP (actively effluxed from cells by ABC Transporter MRP8)

Yet to be accurately represented: p53 to connect DNA damage with cell cycle arrest and apoptosis



*Needed: a p53-Mdm2 model (existing models by Ciliberto, Chickarmane,...) to connect DNA damage with cell cycle arrest at checkpoints and apoptosis* 

#### Future work (or work in progress) for PK-PD models

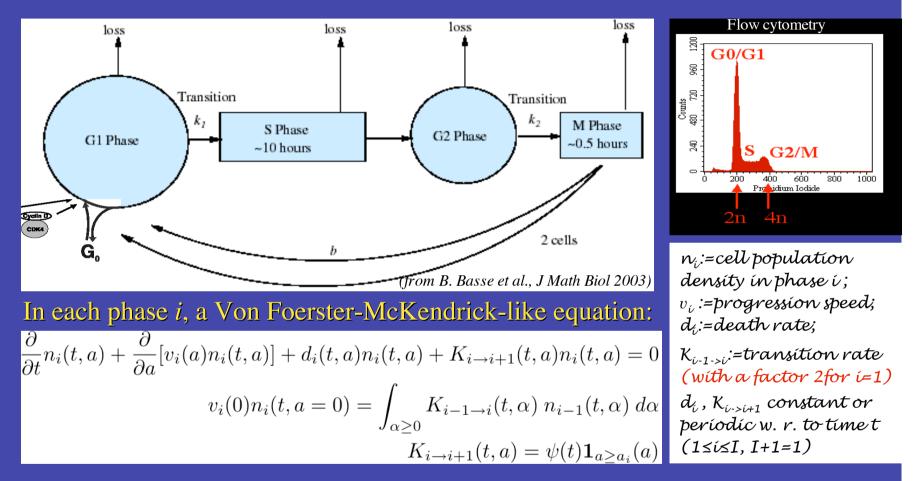
Such molecular (=physiological) modelling should be included in a multiscale whole body physiologically based ("WBPBPKPD") model:

- From the cell to the tissue (cell environment, whole body regulations)
- From the tissue to the whole organism (compartmental modelling)
- From the individual patient to the population (populational PK-PD)

# 2. Modelling cell proliferation and its control mechanisms in cell populations

Age-structured partial differential equations (PDEs)

#### Modelling the cell division cycle in cell populations Age-structured PDE models



Death rates  $d_i$ : ("loss"), "speeds"  $v_i$  and phase transitions  $K_{i->i+1}$  are model targets for physiological (e.g. circadian) and therapeutic (drugs) control  $\psi(t)$ [ $\psi(t)$ : e.g., clock-controlled CDK1 or intracellular output of drug infusion flow] (Firstly presented in: JC, B. Laroche, S. Mischler, B. Perthame, RR INRIA #4892, 2003)

### The simplest case: 1-phase model with division

$$\begin{split} \frac{\partial}{\partial t}n(t,a) &+ \frac{\partial}{\partial a}[n(t,a)] + \left[d(t) + K(t,a)\right]n(t,a) = 0\\ n(t,a=0) &= 2\int_{\alpha \ge 0} K(t,\alpha) \ n(t,\alpha) \ d\alpha\\ \text{where } K(t,a) &= K_0\psi(t)\mathbbm{1}_{[a^*,+\infty[}(a)\\ \text{and } \psi(t) &= \mathbbm{1}_{[0,\tau[}(t),1\text{-periodic}) \end{split}$$

(Here, v(a)=1,  $a^*$  is the cell cycle duration, and  $\tau < 1$  is the time during which the *periodic control*  $\psi$  is actually exerted on cell division)

Then it can be shown that the eigenvalue problem:  $n(t,a) = e^{\lambda t} N(t,a)$ 

$$\begin{aligned} \frac{\partial}{\partial t}N(t,a) &+ \frac{\partial}{\partial a}[N(t,a)] + [\lambda + d(t) + K(t,a)] N(t,a) = 0\\ N(t,a=0) &= 2 \int_{\alpha \ge 0} K(t,\alpha) N(t,\alpha) \ d\alpha \end{aligned}$$

admits a unique *positive* 1-*periodic* eigenvector N, with a *positive* eigenvalue  $\lambda$ , a so-called Malthus exponent, or exponential growth rate for the cell population

General case (I phases): Existence of a nonnegative first eigenvalue  $\lambda$  and, if  $\widetilde{N}_i(t, a) = e^{-\lambda t} n_i(t, a)$ , of eigenvectors  $N_i$ , bounded solutions to the problem :

$$\begin{split} \frac{\partial}{\partial t}N_i(t,a) &+ \frac{\partial}{\partial a}N_i(t,a) + [d_i(t,a) + \lambda + K_{i \to i+1}(t,a)]N_i(t,a) = 0, \\ N_i(t,a=0) &= \int_{\alpha \ge 0} K_{i-1 \to i}(t,\alpha) \ N_{i-1}(t,\alpha) \ d\alpha, \quad 2 \le i \le I \\ N_1(t,a=0) &= 2\int_{\alpha > 0} K_{I \to 1}(t,\alpha) \ N_I(t,\alpha) \ d\alpha, \quad \text{with} \sum_{i=1}^I \int_{a \ge 0} N_i(t,a) da \end{split}$$

with a function  $\rho(a)$  such that the asymptotics of  $\widetilde{N}_i(t,a) = e^{-\lambda t} n_i(t,a)$  follow:

= 1

$$\int_{\alpha \ge 0} \left| \widetilde{N_i}(t,\alpha) - \rho(\alpha) N_i(t,\alpha) \right| \varphi_i(t,\alpha) d\alpha \to 0 \quad \text{as } t \to \infty$$

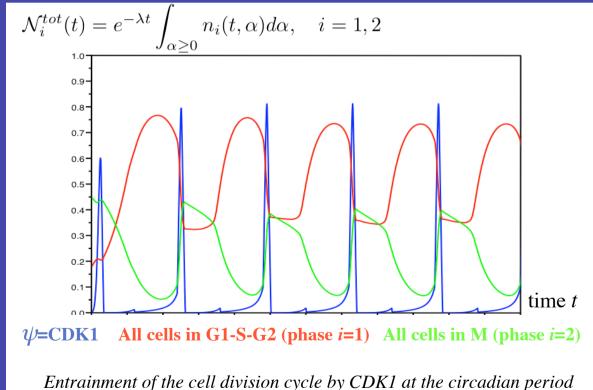
the  $\varphi_i$  being solutions to the dual problem; this can be proved by using an entropy principle (GRE). Moreover, if the control ( $d_i$  or  $K_{i-i+1}$ ) is constant, or if it is periodic, so are the  $N_i$ , with the same period in the periodic case

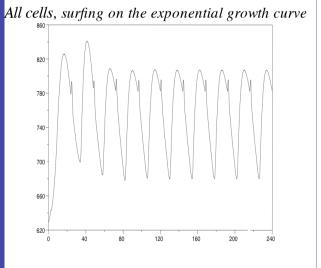
[Term  $d_i + \lambda + K_{i->i+1}$  for the same  $N_i$  to be solutions: the higher the  $d_p$ , the lower the  $\lambda$ ] $\alpha$ Michel, Mischler, Perthame, C. R. Acad. Sci. Paris Ser. I (Math.) 2004; J Math Pures Appl 2005 JC, Michel, Perthame, C. R. Acad. Sci. Paris Ser. I (Math.) 2006; Proc. ECMTB Dresden 2005, Birkhäuser 2007 JC, Gaubert, Perthame, C. R. Acad. Sci. Paris Ser. I (Math.) 2007; JC, Gaubert, Lepoutre, Submitted

# To sum up: a growth exponent for the cell population

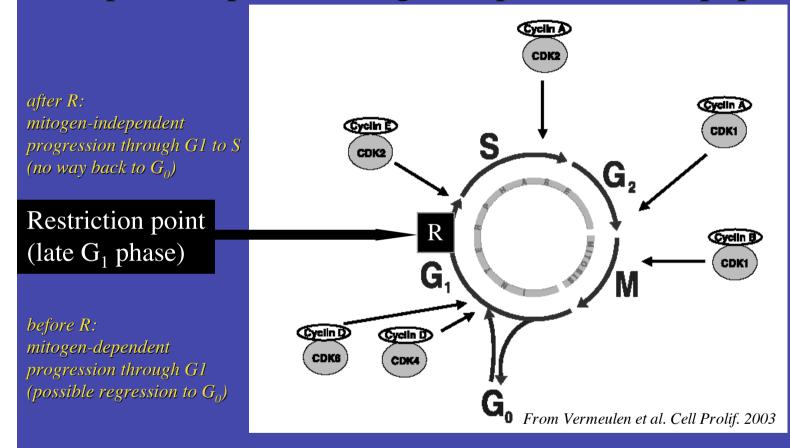
Proof of the existence of a unique growth exponent  $\lambda$ , the same for all phases *i*, such that the  $\widetilde{N}_i(t,a) = e^{-\lambda t} n_i(t,a)$  are asymptotically (i.e., for large times) bounded, and asymptotically periodic if the control is periodic

*Surfing on the exponential growth curve*, example (periodic control case): 2 phases, control on G<sub>2</sub>/M transition by 24-h-periodic CDK1-Cyclin B (A. Goldbeter's model)





# Complementary modelling: exchanges between $G_1$ and $G_0$ phases (proliferating and quiescent cell populations)



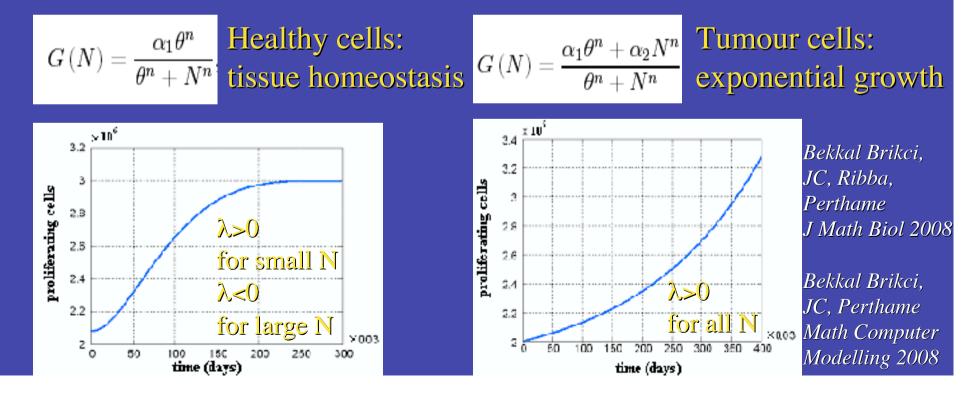
Most cells do not proliferate physiologically, even in fast renewing tissues (e.g. gut) Exchanges between proliferative ( $G_1SG_2M$ ) and quiescent ( $G_0$ ) cell compartments are controlled by mitogens and antimitogenic factors in  $G_1$  phase

#### Exchanges between proliferative (p) and quiescent (q) phases: healthy and tumour tissue cases: G<sub>0</sub> to G<sub>1</sub> recruitment differs

$$\frac{\partial}{\partial t} p(t, a, x) + \frac{\partial}{\partial a} \left( \Gamma_0 p(t, a, x) \right) + \frac{\partial}{\partial x} \left( \Gamma_1 (a, x) p(t, a, x) \right) = \begin{cases} N = \sum p + q \\ \text{(total)} \end{cases}$$

$$- \left( L(a, x) + F(a, x) + d_1 \right) p(t, a, x) + G(N(t)) q(t, a, x) , \qquad \text{number of } \end{aligned}$$

$$\frac{\partial}{\partial t} q(t, a, x) = L(a, x) p(t, a, x) - \left( G(N(t)) + d_2 \right) q(t, a, x) . \qquad \text{time } t )$$



### Work in progress and future work on cell populations

1) Merging the linear (Von Foerster-McKendrick) and non linear (Gyllenberg-Webblike) models, together with cell population synchronisation control on transitions  $K_{i->i+1}$ [and on velocities  $v_i(a)$ ]

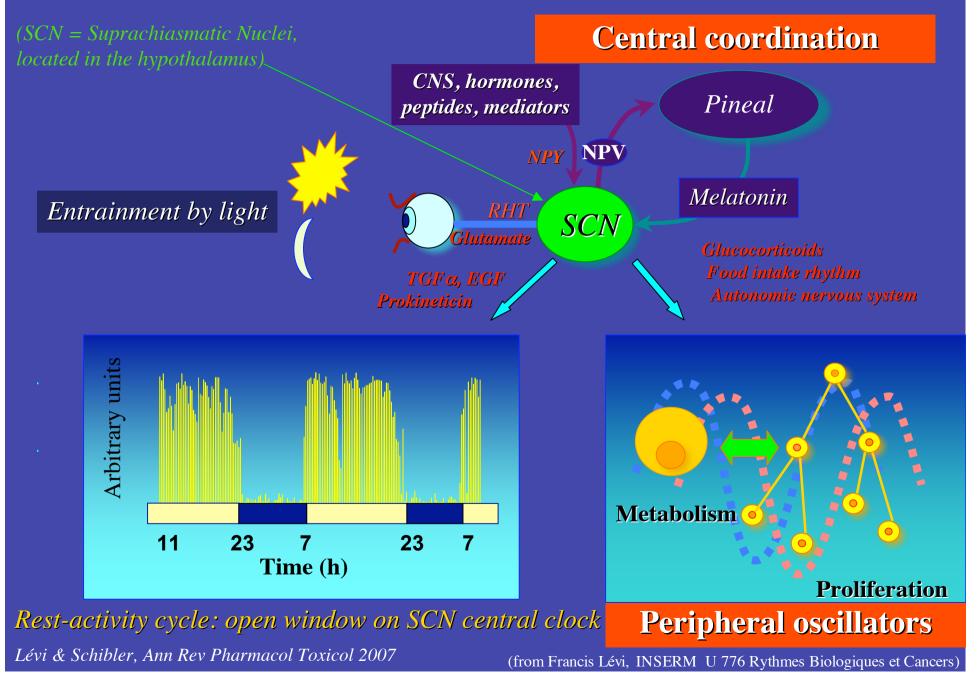
2) Representing the action of different drugs (cytotoxics, EGFR antagonists,...) on molecular-based targets in *various tissue environments*: with mitogens and antimitogens, genomic [in]stability, cell population [de]synchronisation (by *adaptive dynamics equations*?)

#### 3. The circadian system and its disruptions

('Circa diem'=approximately one day)

Representing physiological and disrupted control functions  $\psi_i$  on cell cycle phase transitions ( $G_1/S, G_2/M$ )

### The circadian system



#### The SCN pacemaker as a network of coupled oscillators: Leloup-Goldbeter simplest circadian clock with diffusive coupling between neurons

$$\frac{dmRNA(i)}{dt} = V_s \frac{K^n}{K^n + Z(i)^n} - V_m(i) \frac{mRNA(i)}{K_m + mRNA(i)}$$

$$\frac{dPER(i)}{dt} = k_s mRNA(i) - V_d \frac{PER(i)}{K_d + PER(i)} - k_1 PER(i) + k_2 Z(i) + K_e \sum_{j \neq i} [PER(j) - PER(i)]$$

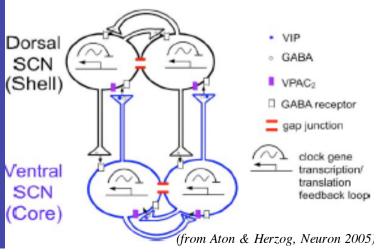
$$\frac{dZ(i)}{K_d + PER(i)} = k_2 Z(i) + K_e \sum_{j \neq i} [PER(j) - PER(i)]$$

 $\frac{l(t)}{lt} = k_1 PER(i) - k_2 Z(i)$ 

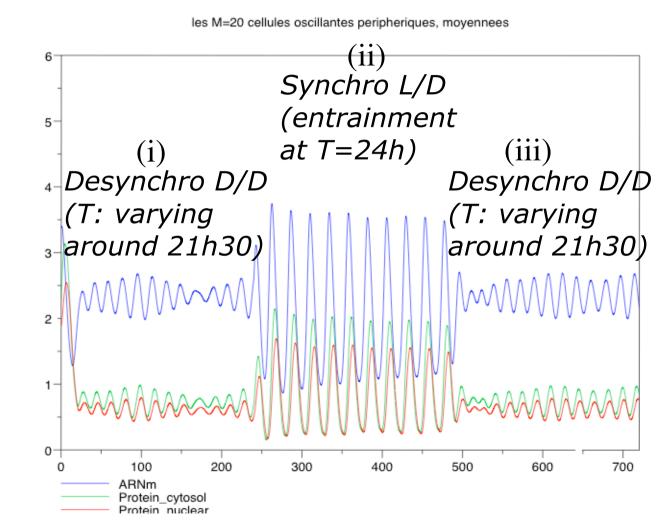
(after Leloup, Gonze, Goldbeter, J Biol Rhythms 1999)

 $V_s: V_s = 1.6 (1 + L \cos(2\pi t/24))$  target of entrainment by light *L*; *K*: target of transcriptional inhibition (e.g. by cytokines);  $V_m(i)$ : the carrier of variabilility of the oscillatory period in this model

3 variables for the i<sup>th</sup> neuron that communicates with all other ( $j \neq i$ ) neurons of the SCN through cytosolic PER protein, with coupling constant  $K_e$ : electric? gap junctions? VIP / VPAC<sub>2</sub> signalling?



# **Result:** example of disrupted clock: averaged *peripheral* oscillator (i) without *central pacemaker* entrainment by light; (ii) with it; (iii) without it again

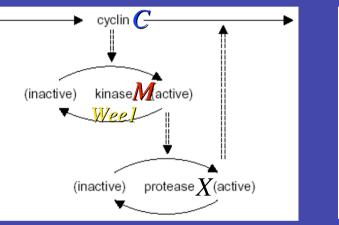


*Resulting Per to control Wee1, that inhibits CDK1* =  $\psi$ , in proliferating cells

JC, Proc. IEEE-EMBC 2006, IEEE-EMB Mag 2008

#### Relating circadian clocks to the cell division cycle ODEs to describe progression in the cell cycle at the single-cell level

A. Golbeter's minimal model for the  $G_2/M$  transition (the « mitotic oscillator »)

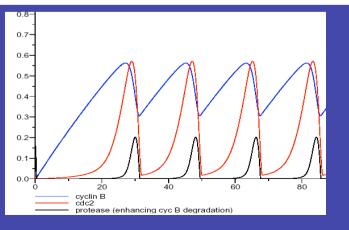


$$\begin{aligned} \frac{\mathrm{d}C}{\mathrm{d}t} &= v_i - k_d C - v_d X \frac{C}{K_d + C} \\ \frac{\mathrm{d}M}{\mathrm{d}t} &= v_1 \frac{C}{K_c + C} \frac{(1 - M)}{K_1 + (1 - M)} - V_2 \frac{M}{K_2 + M} \\ \frac{\mathrm{d}X}{\mathrm{d}t} &= v_3 M \frac{(1 - X)}{K_3 + (1 - X)} - V_4 \frac{X}{K_4 + X}. \end{aligned}$$

C = cyclin B, M = cyclin dependent kinase cdk1, X = degrading protease

Input: Per=Weel; output: M=Cdk1= $\psi$ Switch-like dynamics of dimer Cyclin B-cdk1 Adapted to describe G<sub>2</sub>/M phase transition

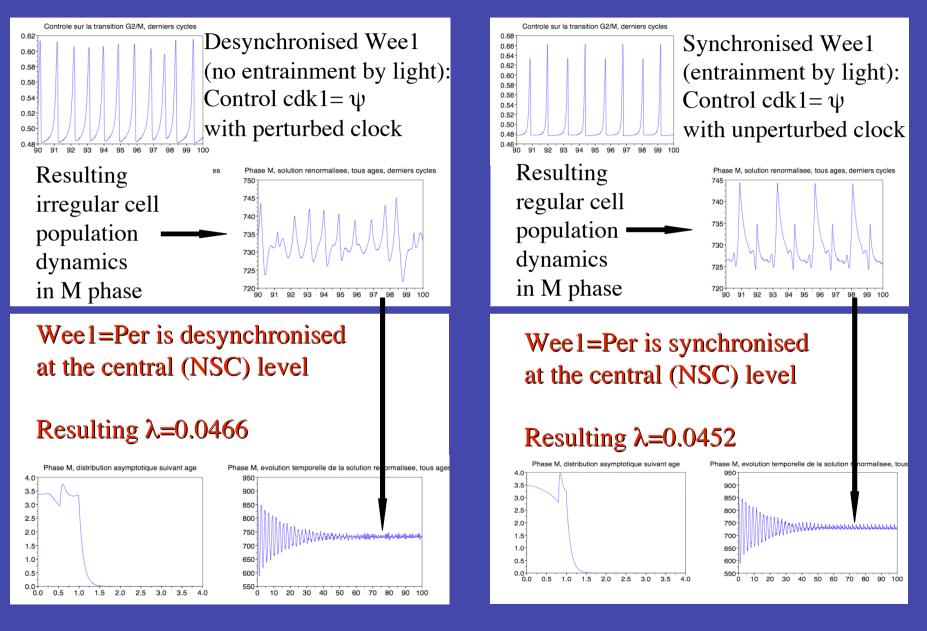
(A. Goldebeter Biochemical oscillations and cellular rhythms, CUP 1996)



Vee

# Clock perturbations and cell population proliferation

(Weel here identified as averaged Per in the circadian clock model)



## 4. Optimisation of anticancer pharmacotherapy

- *1) Objective function* to be minimised: cell population growth rate or cell population density in tumour tissues
- Control function: instantaneous [dynamic] intravenous infusion = [multi-]drug delivery flow via external programmable pumps

#### 3) Constraints to be satisfied:

- maintaining healthy cell population over a tolerability threshold
- taking into account circadian phases of drug processing systems (model prerequisite)
- maintaining normal tissue synchronisation control by circadian clocks
- limiting resistances in tumour cells (e.g. controlling induction of nrf2)
- others: maximal daily dose, maximal delivery flow,...
- 4) With adaptation of drug delivery flow to *patient-specific parameters* (clock phases, enzyme genetic polymorphism, target protein levels,...)

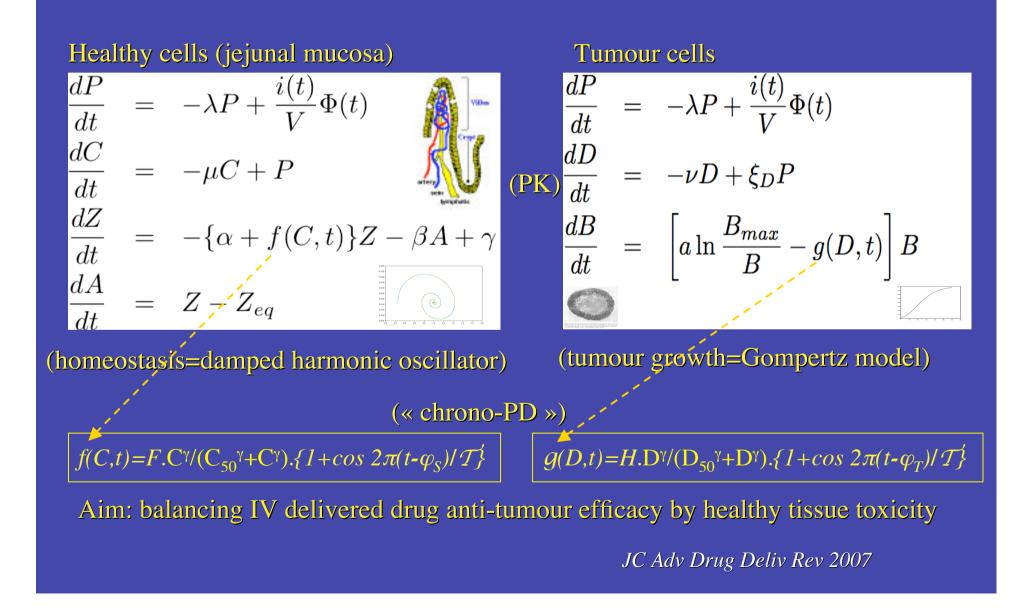
# Drug resistance: a constraint in optimising strategies? Different mechanisms of resistance in tumour cells

- 1. Efflux pumps (ABC transporters): Innate? Acquired: how should they be induced by drugs? (*activation of dormant transporters? Proteic synthesis?*)
- 2. Mutations of the target (*e.g. of BCR-Abl protein for Imatinib resistance*): representation within the frame of PDEs structured according to a genetic trait?
- 3. Overexpression of drug processing enzymes or other detoxicating molecules
- 4. Overexpression of DNA mismatch repair enzymes (resistance to radiotherapy)
- 5. Environmental factors (*micro-*, *e.g.*, *hospicells*; *or macro-*, *e.g.*, *insensitivity to the immune system*)

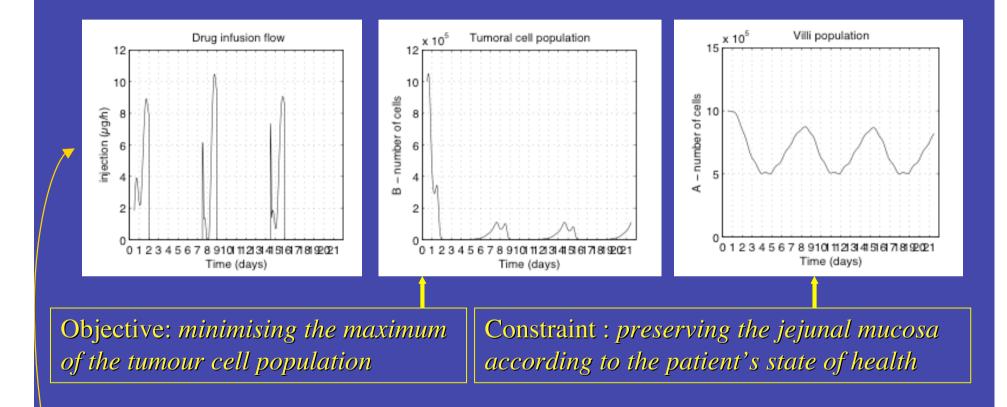
# Example of chronotherapy optimisation with respect to treatment tolerability in a single-drug case

Oxaliplatin to treat Glasgow osteosarcoma in mice, with a jejunal toxicity limit

### PK-PD simplified model for cancer chronotherapy



# Optimal control: results of a tumour stabilisation strategy using this simple PK-PD model



Result : optimal infusion flow adaptable to the patient's state of health (according to a parameter  $\tau_A$ : here preserving at least  $\tau_A = 50\%$  of enterocytes)

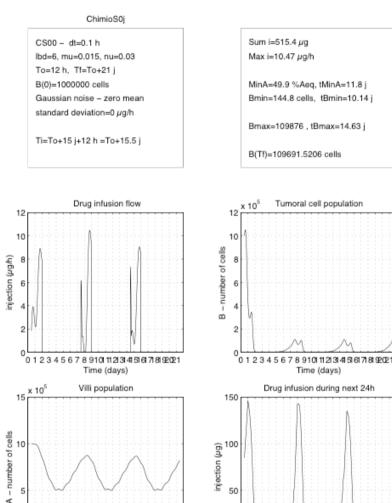
(Basdevant, JC, Lévi, M2AN 2005)

#### Example of treatment adaptation to the patient

For 
$$\tau_{A} = 50$$
 %:

0 1 2 3 4 5 6 7 8 910 112 3 4 5 6 7 8 92021

Time (days)



0123456789101112131415161718192021

Time (days)

Varying  $\tau_A$ :

Numerical results for 1.5 days of infusion + 5.5 days of recovery:

$\tau_{\rm A}$	max B(t)	min B(t)
40 %	28 000	6
50 %	102 000	147
60 %	305 000	2700

 $\tau_A$ = 1- tolerability (the more fragile the patient, the higher is  $\tau_A$ ) 5. Individualising treatments: (circadian profiling, genotyping)

Identifying patient-specific parameters

- a) Circadian clock timing: phases of rhythmic cell cycle determinants (*cyclins*, *p53*) and drug metabolism enzymes (*e.g.*, *DPD*) and molecules (*e.g.* red. Glutathione)
- b) Expression and activity levels of drug processing enzymes (uptake, degradation, efflux, e.g. *DPD*, *UGT1A1*, *P-gp*) and cellular targets (*e.g. TS*, *Topoisomerase I*)
- c) DNA mismatch repair enzyme gene expression (*e.g. ERCC1*, *ERCC2*)

Aim: patient genotyping to individualise optimised drug delivery schedules

... But accurate biomarkers for treatment adaptation are still required!

## Conclusion: ongoing modelling work in 3 directions

- *ODEs* for (as much as possible WBPB) PK-PD modelling to represent the dynamics of drug concentrations in cells and tissues
- Physiologically structured (possibly including space) *PDEs* with prescribed targets to represent cell and tissue proliferation dynamics
- *Optimisation methods* to propose optimal control of [multi-] drug infusion flows, considering possible drug synergies and [innate or acquired] drug resistances
- ...Account being taken in the models of whole body (e.g., circadian) known physiological controls on PK and PD determinants, and individual (patient-specific) parameters to be identified (what biomarkers?) for personalised medicine