

# Data assimilation of velocity fields coming from image processing

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INSTITUT NATIONAL DE RECHERCHE EN INFORMATIQUE ET EN AUTOMATIQUE



#### Context: ASSIMAGE



# ACI ASSIMAGE

- ACI: national research collaboration framework
- Collaboration between 8 French laboratories:
  - INRIA
    - IDOPT (Grenoble) Data assimilation
    - CLIME (Paris) Image processing and data assimilation
    - VISTA (Rennes) Image processing
  - CEMAGREF
    - ETNA (Grenoble) Snow avalanches
    - ENGREF (Montpellier) Hydrology
    - Aerobio (Rennes) Aerology and fluid mechanic
  - CNRS
    - LGGE (Grenoble) Glaciology
    - LEGI (Grenoble) Oceanography
- Extra-collaboration with MHI (Sevastopol) Oceanography



#### **Objectives of ASSIMAGE**

- Study the feasibility and potentiality of assimilation of image data
- Application to geophysical simulation models
- Focus on oceanographic application



#### General objectives: image assimilation



#### Summary of Data Assimilation





#### Image Data Assimilation





#### Problems

• Which images: static or dynamic.

• Image space: adapted to edge representation of particular structures, Lagrangian trajectories, vector field, *etc*.

• Image operator: to project the image space into state variable space.

• **Regularity constraint:** to extract information from images generally rely on a regularity constraint since such problem are often ill-posed.



#### Application to oceanography



#### Interesting problems

- Assimilation of:
  - Circulation velocity
  - Lagrangian trajectories
    - Coming from detection and tracking of structures
    - Velocity field integration
  - Matching of structures coming from image space and model space

# Our goal

- Estimation of surface velocity circulation using satellite images
- Assimilation of estimated speed within a circulation model.
  - → We need to define the most appropriate method to estimate velocity.



#### Simulated data

- OPA: 3D circulation model
- SST
- Velocity field
- Spatial resolution 5km<sup>2</sup>
- Temporal 24h
- Sample test 500km<sup>2</sup>



#### Données simulées





#### Données simulées



SST et Champ de vitesses



# Image processing



#### Motion estimation

• Conservation equation:

$$\frac{dI}{dt}(x, y, t) = \frac{\partial I}{\partial t} + \nabla I \cdot \mathbf{w} + I_t = 0$$

• Regularity constraint to solve the aperture problem



#### Which conservation equation?

Luminance conservation applied to temperature

$$\frac{\partial T}{\partial t} + \nabla T \cdot \mathbf{w} = 0$$

• Temperature conservation

$$\frac{\partial T}{\partial t} + \nabla T \cdot \mathbf{w} = K_T \Delta T$$



### Conclusion

Luminance Conservation: not so bad!
But not respected everywhere

Temperature conservation: equivalent to luminance conservation since horizontal diffusivity is weak.



Which regularity?

1. Gradient norm:

$$\min \int_{image} |\nabla \mathbf{w}|^2$$

2. Div/Curl:

$$\min \int_{image} \alpha \|\nabla \mathrm{div} \mathbf{w}\|^2 + \beta \|\nabla \mathrm{curl} \mathbf{w}\|^2$$



# **Regularity Constraints**

Gradient norm Div / Curl V



#### Results





#### Dealing with real satellite data



# NOAA-AVHRR images of the Black Sea





#### Two consecutive frames in the sequence





#### List of problems

- Clouds
- Geometry of the acquisition
- Sensor saturation
- Strong temporal variation between frames
- Large spatial variation of the local mean



#### Image pre-processing solutions

- Masks for earth, clouds and saturation
- Spatial filtering (correction of the local mean) frame by frame
- Correction of the global mean for the computation of temporal derivatives



# Original image

# Mask for saturation



# Correction



# Result for July 14<sup>th</sup> 1998



#### Data assimilation



#### Principle of data assimilation

• We can write the principle of data assimilation as:

$$\begin{cases} \frac{dX}{dt} = F(X, C)\\ X(0) = V \end{cases}$$

where:

- X corresponds to the state variable of the model
- C is the control vector
- F is the forecast operator
- V is the initial value



#### Sequential data assimilation

• Kalman methods use the forecast value X and  $X_{obs}$  observation to compute the analyse:

$$a = \mathbf{K}[X_{obs} - \mathbf{H}X] + X$$

where  $\mathbf{H}$  is the observation operator.

• Nudging method is a simplification, the Kalman gain matrix  ${f K}$  is replaced by a constant term  $\lambda$ :

$$a = \lambda [X_{obs} - \mathbf{H}X] + X$$

#### Shallow water model

$$\begin{cases} \frac{du}{dt} - fv = g' \frac{\partial h}{\partial x} + \frac{\tau^{(x)}}{\rho_0 h} + A_h \Delta u \\\\ \frac{dv}{dt} + fu = g' \frac{\partial h}{\partial y} + \frac{\tau^{(y)}}{\rho_0 h} + A_h \Delta v \\\\ \frac{\partial h}{\partial t} + \frac{\partial (uh)}{\partial x} + \frac{\partial (vh)}{\partial y} = 0. \end{cases}$$



#### Assimilation of elevation

$$\begin{cases} \frac{du}{dt} - fv = g'\frac{\partial h}{\partial x} + \frac{\tau^{(x)}}{\rho_0 h} + A_h \Delta u \\\\ \frac{dv}{dt} + fu = g'\frac{\partial h}{\partial y} + \frac{\tau^{(y)}}{\rho_0 h} + A_h \Delta v \\\\ \frac{\partial h}{\partial t} + \frac{\partial(uh)}{\partial x} + \frac{\partial(vh)}{\partial y} = \lambda[\xi_d - \xi_m] \end{cases}$$





#### Assimilation of estimated velocity

$$\begin{cases} \frac{du}{dt} -fv = g'\frac{\partial h}{\partial x} + \frac{\tau^{(x)}}{\rho_0 h} + A_h \Delta u \\ +\lambda \left[ \frac{u_{obs}}{\sqrt{u_{obs}^2 + v_{obs}^2}} - \frac{u}{\sqrt{u^2 + v^2}} \right] \times (\sqrt{u^2 + v^2}) \\ \frac{dv}{dt} +fu = g'\frac{\partial h}{\partial y} + \frac{\tau^{(y)}}{\rho_0 h} + A_h \Delta v \\ +\lambda \left[ \frac{v_{obs}}{\sqrt{u_{obs}^2 + v_{obs}^2}} - \frac{v}{\sqrt{u^2 + v^2}} \right] \times (\sqrt{u^2 + v^2}) \\ \frac{\partial h}{\partial t} + \frac{\partial(uh)}{\partial x} + \frac{\partial(vh)}{\partial y} = 0. \end{cases}$$

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#### **Results:**



# Comparison of results with and without assimilation



#### Measure of difference between fields

To quantify the difference between two fields we use two parameters:

• Average angular error:  $\psi = \arccos(\mathbf{w}_1 \cdot \mathbf{w}_2)$ 

• Quadratic vorticity error:  $\zeta = \sqrt{(\zeta_1 - \zeta_2)^2}$ 

where  $\zeta_1$  and  $\zeta_2$  stands for the curl of the two fields.



### Comparison of errors field to field

July 15th 1998		Forecast	Assimilation of elevation	Assimilation of velocity
Observations	Ψ	28,26	28,74	22,51
	ζ	1,41	1,42	1,16
Forecast	ψ		15,76	22,4
	ζ		0,92	1,19
Assimilation	ψ			22,09
of elevation	ζ			1,12

#### Evolution of errors along time



#### Perspectives

- Assimilation of both velocity and elevation
   How to build the correlation matrix?
- Enhance assimilation technique
   Kalman Filtering?
- The assimilation is made in the resolution of the model.

It should be better to do it in the image space.



#### List of questions

- What is the spatial coherence in the model?
- What the influence of holes?
- Why the vector field is so stable with no assimilation, and how explain it is not so stable with velocity assimilation?
- How much the comparison between estimated surface velocity and shallow-water velocity is realistic?
- How quantify error for model, image processing and other observation?

