

[Help](#)

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#include <stdlib.h>
#include "bs1d_std.h"
#include "error_msg.h"
#define PRECISION 1.0e-7 /*Precision for the localization of FD methods*/

static int howard_amer1(double s, NumFunc_1 *p, double t, double r, double divi
                        int N, int M, double theta, double epsilon, double *ptpr
{
    double k, z, vv, l, h, x, alpha, beta, gamma, alpha1, beta1, gamma1, upwind_al
    int i, j, Index;
    double *P, *Obst, *R, *A, *B, *C, *G;
    int *pp;

    /*Memory Allocation*/
    if (N % 2 == 1) N++;
    Obst = malloc((N + 1) * sizeof(double));
    if (Obst == NULL)
        return MEMORY_ALLOCATION_FAILURE;
    A = malloc((N + 1) * sizeof(double));
    if (A == NULL)
        return MEMORY_ALLOCATION_FAILURE;
    B = malloc((N + 1) * sizeof(double));
    if (B == NULL)
        return MEMORY_ALLOCATION_FAILURE;
    C = malloc((N + 1) * sizeof(double));
    if (C == NULL)
        return MEMORY_ALLOCATION_FAILURE;
    R = malloc((N + 1) * sizeof(double));
    if (R == NULL)
        return MEMORY_ALLOCATION_FAILURE;
    P = malloc((N + 1) * sizeof(double));
    if (P == NULL)
        return MEMORY_ALLOCATION_FAILURE;
    G = malloc((N + 1) * sizeof(double));
    if (G == NULL)
        return MEMORY_ALLOCATION_FAILURE;
    pp = malloc((N + 1) * sizeof(int));
    if (pp == NULL)

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    return MEMORY_ALLOCATION_FAILURE;

/*Time Step*/
k = t / (double)M;

/*Space Localisation*/
z = (r - divid) - SQR(sigma) / 2.0;
l = (sigma * sqrt(t) * sqrt(log(1.0 / PRECISION)) + fabs(z) * t);

/*Space Step*/
h = 2.0 * l / (double)N;

/*Peclet Condition-Coefficient of diffusion augmented */
vv = 0.5 * SQR(sigma);
if ((h * fabs(z)) <= vv)
    upwind_alphacoef = 0.5;
else
{
    if (z > 0.) upwind_alphacoef = 0.0;
    else upwind_alphacoef = 1.0;
}
vv -= z * h * (upwind_alphacoef - 0.5);

/*Factor of theta-schema*/
alpha = theta * k * (-vv / (h * h) + z / (2.0 * h));
beta = 1.0 + k * theta * (r + 2.*vv / (h * h));
gamma = k * theta * (-vv / (h * h) - z / (2.0 * h));

alpha1 = k * (1.0 - theta) * (vv / (h * h) - z / (2.0 * h));
beta1 = 1.0 - k * (1.0 - theta) * (r + 2.*vv / (h * h));
gamma1 = k * (1.0 - theta) * (vv / (h * h) + z / (2.0 * h));

/*Terminal Values*/
x = log(s);
for (i = 0; i <= N; i++)
{
    Obst[i] = (p->Compute)(p->Par, exp(x - l + (double)i * h));
    P[i] = Obst[i];
}

/*Finite Difference Cycle*/

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for (i = 1; i <= M; i++)
{
    /*Init Control*/
    for (j = 0; j <= N; j++)
        pp[j] = 0;

    for (j = 1; j < N; j++)
        R[j] = P[j] * beta1 + alpha1 * P[j - 1] + gamma1 * P[j + 1];

    /*Howard Cycle*/
    do
    {
        error = 0.;

        for (j = 1; j < N; j++)
        {
            g0 = P[j - 1] * alpha + P[j] * beta + P[j + 1] * gamma - R[j];
            g1 = P[j] - Obst[j];
            if (g0 < g1) pp[j] = 0;
            else pp[j] = 1;
        }

        for (j = 1; j < N; j++)
        {
            if (pp[j] == 0)
            {
                G[j] = R[j];
                A[j] = alpha;
                B[j] = beta;
                C[j] = gamma;
            }
            else
            {
                G[j] = Obst[j];
                A[j] = 0;
                B[j] = 1;
                C[j] = 0;
            }
        }
    }

    /*Set Gauss*/

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    for (j = N - 2; j >= 1; j--)
        B[j] = B[j] - C[j] * A[j + 1] / B[j + 1];
    for (j = 1; j < N; j++)
        A[j] = A[j] / B[j];
    for (j = 1; j < N - 1; j++)
        C[j] = C[j] / B[j + 1];

    /*Solve the system*/
    for (j = N - 2; j >= 1; j--)
        G[j] = G[j] - C[j] * G[j + 1];

    temp = P[1];
    P[1] = G[1] / B[1];
    error = fabs(P[1] - temp);
    for (j = 2; j < N; j++)
    {
        temp = P[j];
        P[j] = G[j] / B[j] - A[j] * P[j - 1];
        error += fabs(P[j] - temp);
    }
    while (error > epsilon);
    /*End Howard Cycle*/
}
/*End Finite Difference Cycle*/

Index = (int) floor((double)N / 2.0);

/*Price*/
*ptprice = P[Index];

/*Delta*/
*ptdelta = (P[Index + 1] - P[Index - 1]) / (2.0 * s * h);

/*Memory Desallocation*/
free(P);
free(pp);
free(G);
free(A);
free(B);
free(C);

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    free(R);
    free(Obst);

    return OK;
}

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int CALC(FD_Howard_amer1)(void *Opt, void *Mod, PricingMethod *Met)
{
    TYPEOPT *ptOpt = (TYPEOPT *)Opt;
    TYPEMOD *ptMod = (TYPEMOD *)Mod;
    double r, divid;

    r = log(1. + ptMod->R.Val.V_DOUBLE / 100.);
    divid = log(1. + ptMod->Divid.Val.V_DOUBLE / 100.);

    return howard_amer1(ptMod->S0.Val.V_PDOUBLE, ptOpt->PayOff.Val.V_NUMFUNC_1,
                        ptOpt->Maturity.Val.V_DATE - ptMod->T.Val.V_DATE, r, divid,
                        Met->Par[0].Val.V_INT, Met->Par[1].Val.V_INT, Met->Par[2].
                        Met->Par[3].Val.V_RGDOUBLE,
                        &(Met->Res[0].Val.V_DOUBLE), &(Met->Res[1].Val.V_DOUBLE));
}

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static int CHK_OPT(FD_Howard_amer1)(void *Opt, void *Mod)
{
    Option *ptOpt = (Option *)Opt;
    TYPEOPT *opt = (TYPEOPT *) (ptOpt->TypeOpt);

    if ((opt->EuOrAm). Val.V_BOOL == AMER)
        return OK;

    return WRONG;
}

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static int MET(Init)(PricingMethod *Met, Option *Opt)
{

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    if (Met->init == 0)
    {
        Met->init = 1;

        Met->Par[0].Val.V_INT2 = 100;
        Met->Par[1].Val.V_INT2 = 100;
        Met->Par[2].Val.V_RGDOUBLE = 0.5;
        Met->Par[3].Val.V_RGDOUBLE = 0.000001;

    }

    return OK;
}

PricingMethod MET(FD_Howard_amer1) =
{
    "FD_Howard",
    { {"SpaceStepNumber", INT2, {128}, ALLOW},
      {"TimeStepNumber", INT2, {128}, ALLOW},
      {"Theta", RGDOUBLE, {100}, ALLOW},
      {"Epsilon", RGDOUBLE, {100}, ALLOW},
      {" ", PREMIA_NULLTYPE, {0}, FORBID}
    },
    CALC(FD_Howard_amer1),
    { {"Price", DOUBLE, {100}, FORBID},
      {"Delta", DOUBLE, {100}, FORBID} ,
      {" ", PREMIA_NULLTYPE, {0}, FORBID}
    },
    CHK_OPT(FD_Howard_amer1),
    CHK_fdiff,
    MET(Init)
};

```