

[Help](#)

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#include "hes1d_std.h"
#include "enums.h"
#include "pnl/pnl_cdf.h"

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion < (2009+2) //The "#els
static int CHK_OPT(MC_Pelsser_Heston)(void *Opt, void *Mod)
{
    return NONACTIVE;
}
int CALC(MC_Pelsser_Heston)(void *Opt, void *Mod, PricingMethod *Met)
{
    return AVAILABLE_IN_FULL_PREMIA;
}
#else

static double ran_gamma_pdf(const double x, const double a)
{
    double p, lngamma_a;
    if (x < 0)
    {
        return 0 ;
    }
    else if (x == 0)
    {
        if (a == 1)
            return 1. ;
        else
            return 0 ;
    }
    else if (a == 1)
    {
        return exp(-x) ;
    }
    else
    {
        lngamma_a = pnl_lgamma(a);
        p = exp((a - 1) * log(x) - x - lngamma_a);
        return p;
    }
}
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    }
}

static double cdf_gamma_Q(double x, double a)
{
    int which;
    double scale, bound;
    int status;
    double p, q;
    which = 1;
    scale = 1.;

    pnl_cdf_gam(&which, &p, &q, &x, &a, &scale, &status, &bound);
    return q;
}

void cdf_gamma_Qinv_unif_grid(unsigned int N, double *inverse, const double a, c
{
    //we would like to map the inverse of the gamma(a,b) distribution on the grid
    // at step k, a close guess to the inverse of k/N is the invere of (k-1)/N tha
    double lambda, dQ, phi;
    double Q, x;
    double step0, step1, step;
    int i;
    unsigned int j;

    inverse[0] = 0.0;
    {
        Q = 1. - 1. / N;
        x = exp((pnl_lgamma(a) + log(1. - Q)) / a);

        for (i = 0; i < 35; i++) // maximum numer of iteration is 35
        {
            dQ = Q - cdf_gamma_Q(x, a);
            phi = ran_gamma_pdf(x, a);

            if (dQ == 0.0) break;
            else
            {
                lambda = -dQ / MAX(2 * fabs(dQ / x), phi);
                step0 = lambda;
            }
        }
    }
}

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        step1 = -((a - 1) / x - 1) * lambda * lambda / 4.0;
        step = step0;
        if (fabs(step1) < fabs(step0)) step += step1;

        if (x + step > 0) x += step;
        else    x /= 2.0;

        if (fabs(step0) < 1e-10 * x) break;
    }
}
inverse[1] = b * x;
}
for (j = 2; j < N; j++)
{
    Q = 1. - (double)j / N;
    x = inverse[j - 1];

    for (i = 0; i < 35; i++) // maximum numer of iteration is 35
    {
        dQ = Q - cdf_gamma_Q(x, a);
        phi = ran_gamma_pdf(x, a);

        if (dQ == 0.0) break;
        else
        {
            lambda = -dQ / MAX(2 * fabs(dQ / x), phi);
            step0 = lambda;
            step1 = -((a - 1) / x - 1) * lambda * lambda / 4.0;
            step = step0;
            if (fabs(step1) < fabs(step0)) step += step1;

            if (x + step > 0) x += step;
            else    x /= 2.0;

            if (fabs(step0) < 1e-10 * x) break;
        }
    }
    inverse[j] = b * x;
}
}

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//we would like to map the inverse of the chi_squre(nu) distribution on the grid

static void cdf_chisq_Qinv_unif_grid(unsigned int N, double *inverse, const double nu)
{
    cdf_gamma_Qinv_unif_grid(N, inverse, nu / 2, 2.0);
}

static double cdf_chisq_Qinv(double q, double nu)
{
    int which;
    double x, p, bound;
    int status;
    p = 1. - q;
    which = 2;

    pnl_cdf_chi(&which, &p, &q, &x, &nu, &status, &bound);
    return x;
}

int MCPelsser(double S0, NumFunc_1 *pf, double T, double r, double divid, double delta)
{
    double delta;
    int i;
    int j;
    double g1, unif;
    double price_sample, delta_sample, mean_price, mean_delta, var_price, var_delta;
    double alpha, z_alpha;
    double V, log_S;
    double erT;
    double d, ekd, nekd, C0, NN;
    double K1, K2, K3, K4, A, B;
    double C6, C7, C8;
    double K000;
    int Nmax; // nombre maximum de poisson simul
    int N_grid; // Number of grid points nombre d'inverse calcul
    double gamma1, gamma2; // CENTRAL DISCRETIZATION
    double **Cache;
    int N, k;
    double Vi, lambda, gen;
    int pois;

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delta = T / N_t_grid;;
erT = exp((r - divid) * T);
Nmax = 40;
N_grid = 10000;
gamma1 = 0.5;
gamma2 = 0.5;
gen = 0.;

//Memory allocation
Cache = malloc((Nmax + 1) * sizeof(double *));
if (Cache == NULL)
    return MEMORY_ALLOCATION_FAILURE;
for (i = 0; i < Nmax + 1; i++)
{
    Cache[i] = malloc(N_grid * sizeof(double));
    if (Cache[i] == NULL) return MEMORY_ALLOCATION_FAILURE;
}

//Useful constants
d = 4 * K_heston * Theta / (sigma * sigma);
ekd = exp(-K_heston * delta);
nekd = 1. - ekd;
C0 = pow(sigma, 2.) * nekd / (4 * K_heston);
NN = ekd / C0;
K1 = gamma1 * delta * (K_heston * rho / sigma - 0.5) - rho / sigma;
K2 = gamma2 * delta * (K_heston * rho / sigma - 0.5) + rho / sigma;
K3 = gamma1 * delta * (1 - pow(rho, 2.));
K4 = gamma2 * delta * (1 - pow(rho, 2.));

A = K2 + 0.5 * K4;
B = K1 + 0.5 * K3;

C6 = -C0 * A / (1. - 2.*C0 * A);
C7 = 0.5 * d * log(1. - 2.*C0 * A);
C8 = -B;

/* Value to construct the confidence interval */
alpha = (1. - confidence) / 2.;
z_alpha = pn1_inv_cdfnor(1. - alpha);

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/*Initialisation*/
mean_price = 0.0;
mean_delta = 0.0;
var_price = 0.0;
var_delta = 0.0;

pnl_rand_init(generator, 1, N_sample);

//Pre-compute inverse Chi2 on an array
for (N = 0; N < Nmax + 1; N++)
    cdf_chisq_Qinv_unif_grid(N_grid, Cache[N], d + 2 * N);

for (j = 0; j < N_sample; j++)
{
    // N_path Paths
    V = v0;
    log_S = log(S0);
    for (i = 0; i < N_t_grid; i++)
    {
        unif = pnl_rand_uni(generator);
        g1 = pnl_rand_normal(generator);
        Vi = V;
        lambda = NN * Vi;
        pois = pnl_rand_poisson(lambda * 0.5, generator);
        if (pois <= Nmax)
        {
            k = (int)floor(unif * N_grid);
            if (k > N_grid - 2) k = N_grid - 2;
            gen = ((k + 1.) - N_grid * unif) * Cache[pois][k]
                + (N_grid * unif - k) * Cache[pois][k + 1];
        }
        else
        {
            gen = cdf_chisq_Qinv(unif, d + 2 * pois);
        }

        V = C0 * gen;
        K000 = C6 * lambda + C7 + C8 * Vi;
        log_S += K000 + K1 * Vi + K2 * V + sqrt(K3 * Vi + K4 * V) * g1;
    }
}

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    }

    /*Price*/
    price_sample = (pf->Compute)(pf->Par, erT * exp(log_S));

    /* Delta */
    if (price_sample > 0.0)
        delta_sample = (erT * exp(log_S) / S0);
    else delta_sample = 0.;

    /* Sum */
    mean_price += price_sample;
    mean_delta += delta_sample;

    /* Sum of squares */
    var_price += SQR(price_sample);
    var_delta += SQR(delta_sample);

}

/* End of the N iterations */

/* Price estimator */
*ptprice = (mean_price / (double)N_sample);
*pterror_price = exp(-r * T) * sqrt(var_price / (double)N_sample - SQR(*ptprice));
*ptprice = exp(-r * T) * (*ptprice);

/* Price Confidence Interval */
*inf_price = *ptprice - z_alpha * (*pterror_price);
*sup_price = *ptprice + z_alpha * (*pterror_price);

/* Delta estimator */
*ptdelta = exp(-r * T) * (mean_delta / (double)N_sample);
if ((pf->Compute) == &Put)
    *ptdelta *= (-1);
*pterror_delta = sqrt(exp(-2.0 * r * T) * (var_delta / (double)N_sample - SQR(

/* Delta Confidence Interval */
*inf_delta = *ptdelta - z_alpha * (*pterror_delta);
*sup_delta = *ptdelta + z_alpha * (*pterror_delta);

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/*Memory desallocation*/
for (i = 0; i <= Nmax; i++)
    free(Cache[i]);
free(Cache);

return OK;
}

int CALC(MC_Pelsser_Heston)(void *Opt, void *Mod, PricingMethod *Met)
{
    TYPEOPT *ptOpt = (TYPEOPT *)Opt;
    TYPEMOD *ptMod = (TYPEMOD *)Mod;
    double r, divid;

    r = log(1. + ptMod->R.Val.V_DOUBLE / 100.);
    divid = log(1. + ptMod->Divid.Val.V_DOUBLE / 100.);

    return MCPelsser(ptMod->S0.Val.V_PDOUBLE,
        ptOpt->PayOff.Val.V_NUMFUNC_1,
        ptOpt->Maturity.Val.V_DATE - ptMod->T.Val.V_DATE,
        r,
        divid, ptMod->Sigma0.Val.V_PDOUBLE,
        ptMod->MeanReversion.Val.V_PDOUBLE,
        ptMod->LongRunVariance.Val.V_PDOUBLE,
        ptMod->Sigma.Val.V_PDOUBLE,
        ptMod->Rho.Val.V_PDOUBLE,
        Met->Par[0].Val.V_INT,
        Met->Par[1].Val.V_INT,
        Met->Par[2].Val.V_ENUM.value,
        Met->Par[3].Val.V_RGDOUBLE12,
        Met->Par[4].Val.V_PDOUBLE,
        &(Met->Res[0].Val.V_DOUBLE),
        &(Met->Res[1].Val.V_DOUBLE),
        &(Met->Res[2].Val.V_DOUBLE),
        &(Met->Res[3].Val.V_DOUBLE),
        &(Met->Res[4].Val.V_DOUBLE),
        &(Met->Res[5].Val.V_DOUBLE),
        &(Met->Res[6].Val.V_DOUBLE),
        &(Met->Res[7].Val.V_DOUBLE));
}

```



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static int CHK_OPT(MC_Pelsser_Heston)(void *Opt, void *Mod)
{
    if ((strcmp(((Option *)Opt)->Name, "CallEuro") == 0) || (strcmp(((Option *)Opt)
        return OK;

    return WRONG;
}

#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met, Option *Opt)
{
    //int type_generator;
    if (Met->init == 0)
    {
        Met->init = 1;

        Met->Par[0].Val.V_INT = 10000;
        Met->Par[1].Val.V_INT = 4;
        Met->Par[2].Val.V_ENUM.value = 0;
        Met->Par[2].Val.V_ENUM.members = &PremiaEnumMCRNGs;
        Met->Par[3].Val.V_RGDOUBLE12 = 1.5;
        Met->Par[4].Val.V_DOUBLE = 0.95;
    }

    return OK;
}

PricingMethod MET(MC_Pelsser_Heston) =
{
    "MC_Pelsser",
    { {"N iterations", INT, {100}, ALLOW},
      {"TimeStepNumber", INT, {100}, ALLOW},
      {"RandomGenerator", ENUM, {100}, ALLOW},
      {"THRESHOLD", DOUBLE, {100}, ALLOW},
      {"Confidence Value", DOUBLE, {100}, ALLOW},
      {" ", PREMIA_NULLTYPE, {0}, FORBID}
    },
    CALC(MC_Pelsser_Heston),
    { {"Price", DOUBLE, {100}, FORBID},
      {"Delta", DOUBLE, {100}, FORBID} ,

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    {"Error Price", DOUBLE, {100}, FORBID},
    {"Error Delta", DOUBLE, {100}, FORBID} ,
    {"Inf Price", DOUBLE, {100}, FORBID},
    {"Sup Price", DOUBLE, {100}, FORBID} ,
    {"Inf Delta", DOUBLE, {100}, FORBID},
    {"Sup Delta", DOUBLE, {100}, FORBID} ,
    {" ", PREMIA_NULLTYPE, {0}, FORBID}
},
CHK_OPT(MC_Pelsser_Heston),
CHK_mc,
MET(Init)
};
```