

## Help

```

/* Optimal Quantization Algorithm */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <float.h>

#include "bsnd_stdnd.h"
#include "math/linsys.h"
#include "pnl/pnl_basis.h"
#include "black.h"
#include "optype.h"
#include "enums.h"
#include "var.h"
#include "pnl/pnl_random.h"
#include "premia_obj.h"
#include "pnl/pnl_matrix.h"

/* epsilon to detect if continuation value is reached */
#define EPS_CONT 0.0000001

static const double LandMarkNorm = 30;

static double *Q = NULL, *BSQ = NULL, *Weights = NULL, *Trans = NULL, *Price = NULL;
static double *Aux_B = NULL, *Aux_BN = NULL, *Brownian_Bridge = NULL, *Cells_To_LandMark = NULL;
static double *Radius = NULL, *Dist_To_LandMark = NULL, *Sqrt_Inv_Time = NULL;
static int *Number_Cell = NULL;

static int (*Search_Method)(double *S, int Time, int AL_T_Size, long OP_EmBS_Dim, long OP_Exercice_Dates, long AL_MonteCarlo_Iterations)

static int QOpt_Allocation(int AL_T_Size, int BS_Dimension,
                           int OP_Exercice_Dates, long AL_MonteCarlo_Iterations)
{
    if (Tesselation == NULL) Tesselation = (double *)malloc(AL_T_Size * BS_Dimension);
    if (Tesselation == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Radius == NULL) Radius = (double *)malloc(AL_T_Size * sizeof(double));
    if (Radius == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Dist_To_LandMark == NULL) Dist_To_LandMark = (double *)malloc(AL_T_Size * sizeof(double));
    if (Dist_To_LandMark == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Cells_To_LandMark_Up == NULL) Cells_To_LandMark_Up = (double *)malloc(AL_T_Size * sizeof(double));
    if (Cells_To_LandMark_Up == NULL) return MEMORY_ALLOCATION_FAILURE;
}

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    Cells_To_LandMark_Up = (double *)malloc(BS_Dimension * AL_T_Size * sizeof(double));
    if (Cells_To_LandMark_Up == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Cells_To_LandMark_Do == NULL)
        Cells_To_LandMark_Do = (double *)malloc(BS_Dimension * AL_T_Size * sizeof(double));
    if (Cells_To_LandMark_Do == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Q == NULL)
        Q = (double *)malloc(AL_T_Size * OP_Exercice_Dates * BS_Dimension * sizeof(double));
    if (Q == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (BSQ == NULL)
        BSQ = (double *)malloc(AL_T_Size * OP_Exercice_Dates * BS_Dimension * sizeof(double));
    if (BSQ == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Brownian_Bridge == NULL)
        Brownian_Bridge = (double *)malloc(AL_MonteCarlo_Iterations * BS_Dimension * sizeof(double));
    if (Brownian_Bridge == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Number_Cell == NULL)
        Number_Cell = (int *)malloc(AL_MonteCarlo_Iterations * sizeof(int));
    if (Number_Cell == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Trans == NULL)
        Trans = (double *)malloc(AL_T_Size * AL_T_Size * sizeof(double));
    if (Trans == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Weights == NULL)
        Weights = (double *)malloc(AL_T_Size * sizeof(double));
    if (Weights == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Price == NULL)
        Price = (double *)malloc(OP_Exercice_Dates * AL_T_Size * sizeof(double));
    if (Price == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Aux_B == NULL)
        Aux_B = (double *)malloc(BS_Dimension * sizeof(double));
    if (Aux_B == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Aux_BN == NULL)
        Aux_BN = (double *)malloc(BS_Dimension * sizeof(double));
    if (Aux_BN == NULL) return MEMORY_ALLOCATION_FAILURE;
    if (Sqrt_Inv_Time == NULL)
        Sqrt_Inv_Time = (double *)malloc(OP_Exercice_Dates * sizeof(double));
    if (Sqrt_Inv_Time == NULL) return MEMORY_ALLOCATION_FAILURE;
    return OK;
}

static void QOpt_Liberation()
{
    if (Brownian_Bridge != NULL)

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{
    free(Brownian_Bridge);
    Brownian_Bridge = NULL;
}
if (Tesselation != NULL)
{
    free(Tesselation);
    Tesselation = NULL;
}
if (Q != NULL)
{
    free(Q);
    Q = NULL;
}
if (BSQ != NULL)
{
    free(BSQ);
    BSQ = NULL;
}
if (Trans != NULL)
{
    free(Trans);
    Trans = NULL;
}
if (Weights != NULL)
{
    free(Weights);
    Weights = NULL;
}
if (Price != NULL)
{
    free(Price);
    Price = NULL;
}
if (Aux_B != NULL)
{
    free(Aux_B);
    Aux_B = NULL;
}
if (Aux_BN != NULL)
{

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        free(Aux_BN);
        Aux_BN = NULL;
    }
    if (Radius != NULL)
    {
        free(Radius);
        Radius = NULL;
    }
    if (Sqrt_Inv_Time != NULL)
    {
        free(Sqrt_Inv_Time);
        Sqrt_Inv_Time = NULL;
    }
    if (Cells_To_LandMark_Up != NULL)
    {
        free(Cells_To_LandMark_Up);
        Cells_To_LandMark_Up = NULL;
    }
    if (Cells_To_LandMark_Do != NULL)
    {
        free(Cells_To_LandMark_Do);
        Cells_To_LandMark_Do = NULL;
    }
    if (Dist_To_LandMark != NULL)
    {
        free(Dist_To_LandMark);
        Dist_To_LandMark = NULL;
    }
    if (Number_Cell != NULL)
    {
        free(Number_Cell);
        Number_Cell = NULL;
    }
}

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static int NearestCell1D1(double *S, int Time, int AL_T_Size, long OP_EmBS_Di, in
{
    int j, l = 0;
    long ind;
    double min = DBL_MAX, aux;
    /*one dimensional nearest cell search*/

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ind = 0;
for (j = 0; j < AL_T_Size; j++)
{
    aux = fabs(*S - Tessellation[ind]);
    ind += BS_Dimension;
    if (min > aux)
    {
        min = aux;
        l = j;
    }
}
return l;
}

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static int NearestCell(double *S, int Time, int AL_T_Size, long OP_EmBS_Di, int
{
    /*the Brownian Motion S must be normalised. */
    /*used if the fast nearest cell search fails; this event is of very small prob

    int j, k, l = 0;
    double min = DBL_MAX, aux, auxnorm;

    for (j = 0; j < AL_T_Size; j++)
    {
        aux = 0;
        k = 0;

        while ((aux < min) && (k < BS_Dimension))
        {
            auxnorm = S[k] - Tessellation[j * BS_Dimension + k];
            aux += auxnorm * auxnorm;
            k++;
        }

        if (aux < min)
        {
            min = aux;
            l = j;
        }
    }
}

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    return l;
}

static int FastNearestCell(double *S, int Time, int AL_T_Size, long OP_EmBS_Di,
{
    /* The Brownian Motion S must be normalised. */
    /* see the documentation for the explanation of the fast nearest cell search*/
    int j, k, l = -1, m;
    int InegTrue;
    long jmBS_Dim, mmAL_T_Sizepj;
    double min = DBL_MAX, aux, auxnorm;

    for (m = 0; m < BS_Dimension; m++)
    {
        Dist_To_LandMark[m] = 0;
        for (k = 0; k < m; k++)
        {
            Dist_To_LandMark[m] += S[k] * S[k];
        }
        Dist_To_LandMark[m] += (S[m] - LandMarkNorm) * (S[m] - LandMarkNorm);
        for (k = m + 1; k < BS_Dimension; k++)
        {
            Dist_To_LandMark[m] += S[k] * S[k];
        }
    }
    jmBS_Dim = 0;
    for (j = 0; j < AL_T_Size; j++)
    {
        aux = 0;
        k = 0;
        m = 0;
        InegTrue = 1;
        mmAL_T_Sizepj = j;
        do
        {
            InegTrue = (InegTrue) && (Dist_To_LandMark[m] <= Cells_To_LandMark_Up[
            m++;
            mmAL_T_Sizepj += AL_T_Size;

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    }
    while ((InegTrue) && (m < BS_Dimension));

    if (InegTrue)
    {
        while ((aux < min) && (k < BS_Dimension))
        {
            auxnorm = S[k] - Tessellation[jmBS_Dim + k];
            aux += auxnorm * auxnorm;
            k++;
        }
        if (aux < min)
        {
            min = aux;
            l = j;
        }
    }
    jmBS_Dim += BS_Dimension;
}
if (l == -1)
{
    l = NearestCell(S, Time, AL_T_Size, OP_EmBS_Di, BS_Dimension);
    return l;
}
return l;
}

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static int InitTessellation(char *path, char *name, int BS_Dimension, int AL_T_Size)
{
    int i, j, nvl;
    char NameDef[MAX_PATH_LEN];
    FILE *filtes;
    /*load of a file containing an optimal tessellation*/
    NameDef[0] = '\0';

    if (*name == 'd')
    {
        sprintf(NameDef, "%sd%dn%d.tes", path, BS_Dimension, AL_T_Size);
        filtes = fopen(NameDef, "r");
        if (filtes == NULL) return UNABLE_TO_OPEN_FILE;
    }
}

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else
{
    sprintf(NameDef, "%s%s", path, name);
    filtes = fopen(NameDef, "r");
    if (filtes == NULL) return UNABLE_TO_OPEN_FILE;
}
if (BS_Dimension != 1)
{
    nvl = fscanf(filtes, "%s\ n", NameDef);
    nvl = fscanf(filtes, "%s\ n", NameDef);
    nvl = fscanf(filtes, "%s\ n", NameDef);
    nvl = fscanf(filtes, "%s\ n", NameDef);
}
else
{
    nvl = fscanf(filtes, "%s\ n", NameDef);
    nvl = fscanf(filtes, "%s\ n", NameDef);
    nvl = fscanf(filtes, "%s\ n", NameDef);
}
for (i = 0; i < AL_T_Size; i++)
{
    for (j = 0; j < BS_Dimension; j++)
    {
        nvl = fscanf(filtes, "%lf ", Tessellation + i * BS_Dimension + j);
        if (nvl != 1) return BAD_TESSELATION_FORMAT;
    }
    if (BS_Dimension != 1)
    {
        nvl = fscanf(filtes, "%lf ", Radius + i);
        if (nvl != 1) return BAD_TESSELATION_FORMAT;
    }
}
fclose(filtes);
return OK;
}

static void InitLandMark(int BS_Dimension, int AL_T_Size)
{
    int i, j, k;
    double AuxD;

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/*initialization of the distances (landmarks,quantizations points)+/-(cell rad
for (i = 0; i < BS_Dimension; i++)
{
    for (j = 0; j < AL_T_Size; j++)
    {
        AuxD = 0.;
        for (k = 0; k < i; k++)
        {
            AuxD += Tessellation[j * BS_Dimension + k] * Tessellation[j * BS_Dim
        }
        AuxD += (Tessellation[j * BS_Dimension + i] - LandMarkNorm) * (Tesselat
        for (k = i + 1; k < BS_Dimension; k++)
        {
            AuxD += Tessellation[j * BS_Dimension + k] * Tessellation[j * BS_Dim
        }
        AuxD = sqrt(AuxD);
        Cells_To_LandMark_Up[i * AL_T_Size + j] = (AuxD + Radius[j]) * (AuxD +
        Cells_To_LandMark_Do[i * AL_T_Size + j] = (AuxD - Radius[j]) * (AuxD -
    }
}

static void Tesselations_Scale(int AL_T_Size, int OP_Exercise_Dates, int BS_Dime
                                double Step, double *BS_Spot)
{
    int i, j, k;
    double SqrtTime;
    /*scalings of the initial N(0,Id) optimal tessellation*/
    for (j = 1; j < OP_Exercise_Dates; j++)
    {
        SqrtTime = sqrt((double)j * Step);
        for (i = 0; i < AL_T_Size; i++)
        {
            for (k = 0; k < BS_Dimension; k++)
            {
                Q[i * OP_Exercise_Dates * BS_Dimension + j * BS_Dimension + k] = S
            }
            BlackScholes_Transformation((double)j * Step, BSQ + i * OP_Exercise_Da
        }
    }
}

```

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static void
Compute_Transition(long AL_MonteCarlo_Iterations, int AL_T_Size, int BS_Dimension,
                   int OP_EmBS_Di, int OP_Exercise_Dates, int Time, double Sqrt_Inv_Time)
{
    int i, j, k, AuxNumCell;
    long l;

    for (i = 0; i < AL_T_Size; i++)
    {
        Weights[i] = 0.;
        for (j = 0; j < AL_T_Size; j++)
        {
            Trans[i * AL_T_Size + j] = 0.;
        }
    }

    /*computation of the brownian bridge transition probabilities from the quantization*/
    for (l = 0; l < AL_MonteCarlo_Iterations; l++)
    {
        for (k = 0; k < BS_Dimension; k++)
        {
            Aux_B[k] = Sqrt_Inv_Time * Brownian_Bridge[l * BS_Dimension + k];
        }
        AuxNumCell = Search_Method(Aux_B, Time, AL_T_Size, OP_EmBS_Di, BS_Dimension);

        Trans[AuxNumCell * AL_T_Size + Number_Cell[l]] += 1.;
        Weights[AuxNumCell] += 1.;
        Number_Cell[l] = AuxNumCell;
    }

    /*normalization*/
    for (i = 0; i < AL_T_Size; i++)
    {
        for (j = 0; j < AL_T_Size; j++)
        {
            if (Weights[i] > 0.)
                Trans[i * AL_T_Size + j] /= Weights[i];
        }
    }
}

static void Close()

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{
    /*memory liberation*/
    QOpt_Liberation();
    End_BS();
}

/*see the documentation for the parameters meaning*/
static int QOpt(PnlVect *BS_Spot,
                NumFunc_nd *p,
                double OP_Maturity,
                double BS_Interest_Rate,
                PnlVect *BS_Dividend_Rate,
                PnlVect *BS_Volatility,
                double *BS_Correlation,
                long AL_MonteCarlo_Iterations,
                int generator,
                int OP_Exercise_Dates,
                int AL_T_Size,
                char *AL_Tessellation_Path,
                char *AL_Tessellation_Name,
                double *AL_FPrice,
                double *AL_BPrice)
{
    int i, j, k, AuxNumCell, init_mc, init;
    long l;
    int BS_Dimension = BS_Spot->size;
    long OP_ExmBS_Di = (long)OP_Exercise_Dates * BS_Dimension;
    double Step, Sqrt_Step, DiscountStep, aux;
    PnlVect VStock;
    VStock.size = BS_Dimension;

    /* MC sampling */
    init_mc = pnl_rand_init(generator, BS_Dimension, AL_MonteCarlo_Iterations);

    /* Test after initialization for the generator */
    if (init_mc != OK) return init_mc;

    /*time step*/
    Step = OP_Maturity / (double)(OP_Exercise_Dates - 1);
    Sqrt_Step = sqrt(Step);
    /*discounting factor for a time step*/

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DiscountStep = exp(-BS_Interest_Rate * Step);

/*memory allocation of the BlackScholes variables*/
init = Init_BS(BS_Dimension, BS_Volatility->array,
               BS_Correlation, BS_Interest_Rate, BS_Dividend_Rate->array);
if (init != OK) return init;
/*memory allocation of the algorithm's variables*/
init = QOpt_Allocation(AL_T_Size, BS_Dimension, OP_Exercice_Dates, AL_MonteCar
if (init != OK) return init;

if (BS_Dimension == 1) Search_Method = NearestCell1D1;
else Search_Method = FastNearestCell;

for (j = 1; j < OP_Exercice_Dates; j++)
    Sqrt_Inv_Time[j] = 1. / sqrt((double)j * Step);

/*initialization of the optimal quantizers*/
init = InitTessellation(AL_Tessellation_Path, AL_Tessellation_Name, BS_Dimension,
if (init != OK) return init;
/*landmarks initialization for the fast nearest cell search procedure*/
if (BS_Dimension > 1)
    InitLandMark(BS_Dimension, AL_T_Size);

/*optimal tessellation scalings*/
Tessellations_Scale(AL_T_Size, OP_Exercice_Dates, BS_Dimension, Step, BS_Spot->
/*initialization of the brownian bridge at the maturity*/
Init_Brownian_Bridge(Brownian_Bridge, AL_MonteCarlo_Iterations, BS_Dimension,
/*initialisation of the dynamical programming prices at the maturity*/
for (i = 0; i < AL_T_Size; i++)
{
    VStock.array = BSQ + i * OP_Exercice_Dates * BS_Dimension + (OP_Exercice_D
    Price[(OP_Exercice_Dates - 1)*AL_T_Size + i] = p->Compute(p->Par, &VStock)
}
/*quantization of the brownian bridge*/
for (i = 0; i < AL_MonteCarlo_Iterations; i++)
{
    /*normalisation for the nearest cell search procedure*/
    for (k = 0; k < BS_Dimension; k++)
    {
        Aux_B[k] = Sqrt_Inv_Time[OP_Exercice_Dates - 1] * Brownian_Bridge[i *
    }
}

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        /*nearest cell search*/
        Number_Cell[i] = Search_Method(Aux_B, OP_Exercise_Dates - 1, AL_T_Size, OP
    }
    /*dynamical programming algorithm*/
    for (i = OP_Exercise_Dates - 2; i >= 1; i--)
    {
        /*computation of the brownian bridge at time i*/
        Compute_Brownian_Bridge(Brownian_Bridge, i * Step, Step, BS_Dimension, AL_
        /*computation of the quantized transition kernel of the brownian bridge be
        Compute_Transition(AL_MonteCarlo_Iterations, AL_T_Size, BS_Dimension, OP_E
        /*approximation of the conditionnal expectations*/
        for (j = 0; j < AL_T_Size; j++)
        {
            aux = 0;
            for (k = 0; k < AL_T_Size; k++)
            {
                aux += Price[(i + 1) * AL_T_Size + k] * Trans[j * AL_T_Size + k];
            }
            /*discounting for a time step*/
            aux *= DiscountStep;
            /*aux contains the continuation value at quantization point j and time
            /*exercise decision*/
            VStock.array = BSQ + j * OP_Exercise_Dates * BS_Dimension + i * BS_Dim
            Price[i * AL_T_Size + j] = MAX(p->Compute(p->Par, &VStock), aux);
        }
    }

    aux = 0;
    for (k = 0; k < AL_T_Size; k++)
    {
        aux += Price[AL_T_Size + k] * Weights[k];
    }
    aux /= (double)AL_MonteCarlo_Iterations;
    aux *= DiscountStep;
    /*output backward price*/
    *AL_BPrice = MAX(p->Compute(p->Par, BS_Spot), aux);

    /* Forward price */
    *AL_FPrice = 0.;
    if (*AL_BPrice == p->Compute(p->Par, BS_Spot))
    {

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        *AL_FPrice = *AL_BPrice;
    }
    else
    {
        double payoff;
        for (l = 0; l < AL_MonteCarlo_Iterations; l++)
        {
            /*spot of the brownian motion*/
            for (k = 0; k < BS_Dimension; k++) Aux_B[k] = 0.;
            i = 0;
            /*optimal stopping for a quantized path*/
            do
            {
                i++;
                for (k = 0; k < BS_Dimension; k++)
                {
                    Aux_B[k] += Sqrt_Step * pnl_rand_normal(generator);
                    /*normalization of Aux_B*/
                    Aux_BN[k] = Sqrt_Inv_Time[i] * Aux_B[k];
                }
                /*search of the Aux_BN number cell*/
                AuxNumCell = Search_Method(Aux_BN, i, AL_T_Size, OP_Exercice_Dates);
                VStock.array = BSQ + AuxNumCell * OP_Exercice_Dates * BS_Dimension;
                payoff = p->Compute(p->Par, &VStock);
            }
            while (payoff < Price[i * AL_T_Size + AuxNumCell] - EPS_CONT);
            /*MonteCarlo formulae for the forward price*/
            VStock.array = BSQ + AuxNumCell * OP_Exercice_Dates * BS_Dimension + i *
                *AL_FPrice += Discount(i * Step, BS_Interest_Rate) * (p->Compute(p->Par, &VStock));
        }
        /*output forward price*/
        *AL_FPrice /= (double)AL_MonteCarlo_Iterations;
    }
    Close();
    return OK;
}

int CALC(MC_QuantizationND)(void *Opt, void *Mod, PricingMethod *Met)
{
    TYPEOPT *ptOpt = (TYPEOPT *)Opt;

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TYPEMOD *ptMod = (TYPEMOD *)Mod;
double r;
int i, res;
double *BS_cor;
PnlVect *divid = pnl_vect_create(ptMod->Size.Val.V_PINT);
char tes[MAX_PATH_LEN];
char *file = "d";
PnlVect *spot, *sig;

spot = pnl_vect_compact_to_pnl_vect(ptMod->S0.Val.V_PNLVECTCOMPACT);
sig = pnl_vect_compact_to_pnl_vect(ptMod->Sigma.Val.V_PNLVECTCOMPACT);

for (i = 0; i < ptMod->Size.Val.V_PINT; i++)
    pnl_vect_set(divid, i,
                  log(1. + pnl_vect_compact_get(ptMod->Divid.Val.V_PNLVECTCOMPACT, i)));

r = log(1. + ptMod->R.Val.V_DOUBLE / 100.);

if ((BS_cor = malloc(ptMod->Size.Val.V_PINT * ptMod->Size.Val.V_PINT * sizeof(double))) == NULL)
    return MEMORY_ALLOCATION_FAILURE;
for (i = 0; i < ptMod->Size.Val.V_PINT * ptMod->Size.Val.V_PINT; i++)
    BS_cor[i] = ptMod->Rho.Val.V_DOUBLE;
for (i = 0; i < ptMod->Size.Val.V_PINT; i++)
    BS_cor[i * ptMod->Size.Val.V_PINT + i] = 1.0;

/* path name for the tessellation file*/
strcpy(tes, premia_data_dir);
strcat(tes, "/");
strcat(tes, "tes");
strcat(tes, "/");

res = QOpt(spot,
            ptOpt->PayOff.Val.V_NUMFUNC_ND,
            ptOpt->Maturity.Val.V_DATE - ptMod->T.Val.V_DATE,
            r, divid, sig,
            BS_cor,
            Met->Par[0].Val.V_LONG,
            Met->Par[1].Val.V_ENUM.value,
            Met->Par[2].Val.V_INT,
            Met->Par[3].Val.V_INT,

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        tes,
        file,
        &(Met->Res[0].Val.V_DOUBLE),
        &(Met->Res[1].Val.V_DOUBLE));
    pnl_vect_free(&divid);
    pnl_vect_free(&spot);
    pnl_vect_free(&sig);

    free(BS_cor);

    return res;
}

static int CHK_OPT(MC_QuantizationND)(void *Opt, void *Mod)
{
    Option *ptOpt = (Option *)Opt;
    TYPEOPT *opt = (TYPEOPT *) (ptOpt->TypeOpt);

    if ((opt->EuOrAm).Val.V_BOOL == AMER)
        return OK;
    else
        return WRONG;
}

static int MET(Init)(PricingMethod *Met, Option *Opt)
{
    if (Met->init == 0)
    {
        Met->init = 1;
        Met->Par[0].Val.V_LONG = 10000;
        Met->Par[1].Val.V_ENUM.value = 0;
        Met->Par[1].Val.V_ENUM.members = &PremiaEnumMCRNGs;
        Met->Par[2].Val.V_INT = 10;
        Met->Par[3].Val.V_INT = 200;
    }
    return OK;
}

PricingMethod MET(MC_QuantizationND) =
{

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"MC_Quantization_nd",
{ {"N iterations", LONG, {100}, ALLOW},
  {"RandomGenerator", ENUM, {100}, ALLOW},
  {"Number of Exercise Dates", INT, {100}, ALLOW},
  {"Tesselation Size", INT, {100}, ALLOW},
  {" ", PREMIA_NULLTYPE, {0}, FORBID}
},
CALC(MC_QuantizationND),
{ {"Forward Price", DOUBLE, {100}, FORBID}, {"Backward Price", DOUBLE, {100},
  {" ", PREMIA_NULLTYPE, {0}, FORBID}
},
CHK_OPT(MC_QuantizationND),
CHK_mc,
MET(Init)
};

#undef EPS_CONT

```