

[Help](#)

```
#include "heshwld_std.h"
#include "enums.h"
#include "error_msg.h"

#include "pnl/pnl_random.h"
#include "pnl/pnl_cdf.h"

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion < (2015+2) //The "#els
static int CHK_OPT(MC_HybridTree)(void *Opt, void *Mod)
{
    return NONACTIVE;
}
int CALC(MC_HybridTree)(void *Opt, void *Mod, PricingMethod *Met)
{
    return AVAILABLE_IN_FULL_PREMIA;
}
#else

static double **V,**Q;
static double **y,**f;
static int **f_down,**f_up;
static int **y_down,**y_up;
static double **pu_y,**pd_y;
static double **pu_f,**pd_f;
static double **r,**discount;
static double *initial_yield;

/*ZCB Data*/
static double* tm; /*Times T of maturities read in the file initialyield.dat */
static double* Pm; /*Values of the zero coupon P(0,tm) read in the file initialyi
int n_price1;

static double *shift,*Pc;
static char *init_tr;

/*Memory Allocation*/
static int memory_allocation(int Nt)
{
```

```
int i;
shift= (double *)malloc((Nt+1)*sizeof(double));
initial_yield= (double *)malloc((Nt+2)*sizeof(double));
Pc= (double *)malloc((Nt+2)*sizeof(double));

r=(double**)calloc(Nt+1,sizeof(double*));
if (r==NULL)
    return MEMORY_ALLOCATION_FAILURE;
for (i=0;i<Nt+1;i++)
{
    r[i]=(double *)calloc(Nt+1,sizeof(double));
    if (r[i]==NULL)
        return MEMORY_ALLOCATION_FAILURE;
}

discount=(double**)calloc(Nt+1,sizeof(double*));
if (discount==NULL)
    return MEMORY_ALLOCATION_FAILURE;
for (i=0;i<Nt+1;i++)
{
    discount[i]=(double *)calloc(Nt+1,sizeof(double));
    if (discount[i]==NULL)
        return MEMORY_ALLOCATION_FAILURE;
}

V=(double**)calloc(Nt+1,sizeof(double*));
if (V==NULL)
    return MEMORY_ALLOCATION_FAILURE;
for (i=0;i<Nt+1;i++)
{
    V[i]=(double *)calloc(Nt+1,sizeof(double));
    if (V[i]==NULL)
        return MEMORY_ALLOCATION_FAILURE;
}

Q=(double**)calloc(Nt+1,sizeof(double*));
if (Q==NULL)
    return MEMORY_ALLOCATION_FAILURE;
for (i=0;i<Nt+1;i++)
{
    Q[i]=(double *)calloc(Nt+1,sizeof(double));
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        if (Q[i]==NULL)
            return MEMORY_ALLOCATION_FAILURE;
    }

    pu_y=(double**)calloc(Nt+1,sizeof(double*));
    if (pu_y==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    for (i=0;i<Nt+1;i++)
    {
        pu_y[i]=(double *)calloc(Nt+1,sizeof(double));
        if (pu_y[i]==NULL)
            return MEMORY_ALLOCATION_FAILURE;
    }

    pd_y=(double**)calloc(Nt+1,sizeof(double*));
    if (pd_y==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    for (i=0;i<Nt+1;i++)
    {
        pd_y[i]=(double *)calloc(Nt+1,sizeof(double));
        if (pd_y[i]==NULL)
            return MEMORY_ALLOCATION_FAILURE;
    }

    pu_f=(double**)calloc(Nt+1,sizeof(double*));
    if (pu_f==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    for (i=0;i<Nt+1;i++)
    {
        pu_f[i]=(double *)calloc(Nt+1,sizeof(double));
        if (pu_f[i]==NULL)
            return MEMORY_ALLOCATION_FAILURE;
    }

    pd_f=(double**)calloc(Nt+1,sizeof(double*));
    if (pd_f==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    for (i=0;i<Nt+1;i++)
    {
        pd_f[i]=(double *)calloc(Nt+1,sizeof(double));
        if (pd_f[i]==NULL)
```

```
        return MEMORY_ALLOCATION_FAILURE;
    }

    y=(double**)calloc(Nt+1,sizeof(double*));
    if (y==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    for (i=0;i<Nt+1;i++)
    {
        y[i]=(double *)calloc(Nt+1,sizeof(double));
        if (y[i]==NULL)
            return MEMORY_ALLOCATION_FAILURE;
    }

    f=(double**)calloc(Nt+1,sizeof(double*));
    if (f==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    for (i=0;i<Nt+1;i++)
    {
        f[i]=(double *)calloc(Nt+1,sizeof(double));
        if (f[i]==NULL)
            return MEMORY_ALLOCATION_FAILURE;
    }

    f_down=(int**)calloc(Nt+1,sizeof(int*));
    if (f_down==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    for (i=0;i<Nt+1;i++)
    {
        f_down[i]=(int *)calloc(Nt+1,sizeof(int));
        if (f_down[i]==NULL)
            return MEMORY_ALLOCATION_FAILURE;
    }

    f_up=(int**)calloc(Nt+1,sizeof(int*));
    if (f_up==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    for (i=0;i<Nt+1;i++)
    {
        f_up[i]=(int *)calloc(Nt+1,sizeof(int));
        if (f_up[i]==NULL)
            return MEMORY_ALLOCATION_FAILURE;
    }
```

```
    }

    y_down=(int**)calloc(Nt+1,sizeof(int*));
    if (y_down==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    for (i=0;i<Nt+1;i++)
    {
        y_down[i]=(int *)calloc(Nt+1,sizeof(int));
        if (y_down[i]==NULL)
            return MEMORY_ALLOCATION_FAILURE;
    }

    y_up=(int**)calloc(Nt+1,sizeof(int*));
    if (y_up==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    for (i=0;i<Nt+1;i++)
    {
        y_up[i]=(int *)calloc(Nt+1,sizeof(int));
        if (y_up[i]==NULL)
            return MEMORY_ALLOCATION_FAILURE;
    }

    return OK;
}

static void free_memory(int Nt)
{
    int i;

    free(shift);
    free(initial_yield);
    free(Pc);

    for (i=0;i<Nt+1;i++)
        free(r[i]);
    free(r);

    for (i=0;i<Nt+1;i++)
        free(discount[i]);
    free(discount);
}
```

```
for (i=0;i<Nt+1;i++)
    free(V[i]);
free(V);

for (i=0;i<Nt+1;i++)
    free(Q[i]);
free(Q);

for (i=0;i<Nt+1;i++)
    free(pu_y[i]);
free(pu_y);

for (i=0;i<Nt+1;i++)
    free(pd_y[i]);
free(pd_y);

for (i=0;i<Nt+1;i++)
    free(y[i]);
free(y);

for (i=0;i<Nt+1;i++)
    free(y_up[i]);
free(y_up);

for (i=0;i<Nt+1;i++)
    free(y_down[i]);
free(y_down);

for (i=0;i<Nt+1;i++)
    free(pu_f[i]);
free(pu_f);

for (i=0;i<Nt+1;i++)
    free(pd_f[i]);
free(pd_f);

for (i=0;i<Nt+1;i++)
    free(f[i]);
free(f);
```

```

    for (i=0;i<Nt+1;i++)
        free(f_up[i]);
    free(f_up);

    for (i=0;i<Nt+1;i++)
        free(f_down[i]);
    free(f_down);

    return;
}

static double compute_f(double r, double omega)
{
    return 2.*sqrt(r) / omega;
}

static double compute_v(double R, double omega)
{
    double val;

    val = SQR(R) * SQR(omega) / 4.;
    if (R > 0.)
        val = SQR(R) * SQR(omega) / 4.;
    else
        val = 0.0;
    return val;
}

/*Calibration of the tree v*/
static int tree_v(double tt, double v02, double kappa2, double theta2, double om
{
    int i, j;
    int z;
    double Ru, Rd;
    double mu_r, v_curr;
    double dt, sqrt_dt;

    /*Fixed tree for R=f*/
    f[0][0] = compute_f(v02, omega2);

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dt = tt / (double)Nt;
sqrt_dt = sqrt(dt);

V[0][0] = compute_v(f[0][0], omega2);
f[1][0] = f[0][0] - sqrt_dt;
f[1][1] = f[0][0] + sqrt_dt;
V[1][0] = compute_v(f[1][0], omega2);
V[1][1] = compute_v(f[1][1], omega2);
for (i = 1; i < Nt; i++)
    for (j = 0; j <= i; j++)
    {
        f[i + 1][j] = f[i][j] - sqrt_dt;
        f[i + 1][j + 1] = f[i][j] + sqrt_dt;
        V[i + 1][j] = compute_v(f[i + 1][j], omega2);
        V[i + 1][j + 1] = compute_v(f[i + 1][j + 1], omega2);
    }

for (i = 1; i < Nt; i++)
    for (j = 0; j <= i; j++)

        /*Evolve tree for f*/
        for (i = 0; i < Nt; i++)
        {
            for (j = 0; j <= i; j++)
            {
                /*Compute mu_f*/
                v_curr = V[i][j];

                mu_r = kappa2 * (theta2 - v_curr);

                z = 0;
                while ((V[i][j] + mu_r * dt < V[i + 1][j - z])
                    && (j - z >= 0))
                {
                    z = z + 1;
                }
                f_down[i][j] = -z;
                Rd = V[i + 1][j - z];
            }
        }
    }

```



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    if (z > 0)
        z = 0;
    else z = 1;

    while ((V[i][j] + mu_r * dt > V[i + 1][j + z])
           && (j + z <= i))
    {
        z = z + 1;
    }

    Ru = V[i + 1][j + z];

    f_up[i][j] = z;
    pu_f[i][j] = (V[i][j] + mu_r * dt - Rd) / (Ru - Rd);

    if ((Ru - 1.e-9 > V[i + 1][i + 1]) || (j + f_up[i][j] > i + 1))
    {
        pu_f[i][j] = 1;

        f_up[i][j] = i + 1 - j;
        f_down[i][j] = i - j;
    }
    if ((Rd + 1.e-9 < V[i + 1][0]) || (j + f_down[i][j] < 0))
    {
        pu_f[i][j] = 0.;
        f_up[i][j] = 1 - j;
        f_down[i][j] = 0 - j;
    }
    pd_f[i][j] = 1. - pu_f[i][j];
}
}
return 1;
}

```

```

/*Calibration of the tree the interest rate r Hwicek model*/
static int tree_r(double tt, double r0, double kappa, double omega, int Nt)
{
    int i, j;
    int z;
    double Ru, Rd;

```

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double dt, sqrt_dt;
double mu_r, v_curr;

y[0][0] = 0.;

dt = tt / (double)Nt;
sqrt_dt = sqrt(dt);

y[1][0] = y[0][0] - sqrt_dt;
y[1][1] = y[0][0] + sqrt_dt;

for (i = 1; i < Nt; i++)
    for (j = 0; j <= i; j++)
    {
        y[i + 1][j] = y[i][j] - sqrt_dt;
        y[i + 1][j + 1] = y[i][j] + sqrt_dt;
    }

/*Evolve tree for f*/
for (i = 0; i < Nt; i++)
{
    for (j = 0; j <= i; j++)
    {
        /*Compute mu_f*/
        v_curr = y[i][j];

        mu_r = -kappa * v_curr;

        z = 0;
        while ((y[i][j] + mu_r * dt < y[i + 1][j - z])
            && (j - z >= 0))
        {
            z = z + 1;
        }
        y_down[i][j] = -z;
        Rd = y[i + 1][j - z];

        if (z > 0)
            z = 0;
        else z = 1;
    }
}

```

```

while ((y[i][j] + mu_r * dt > y[i + 1][j + z])
      && (j + z <= i))
{
    z = z + 1;
}

Ru = y[i + 1][j + z];

y_up[i][j] = z;

pu_y[i][j] = (y[i][j] + mu_r * dt - Rd) / (Ru - Rd);

if ((Ru - 1.e-9 > y[i + 1][i + 1]) || (j + y_up[i][j] > i + 1))
{
    pu_y[i][j] = 1;

    y_up[i][j] = i + 1 - j;
    y_down[i][j] = i - j;
}
if ((Rd + 1.e-9 < y[i + 1][0]) || (j + y_down[i][j] < 0))
{
    pu_y[i][j] = 0.;
    y_up[i][j] = 1 - j;
    y_down[i][j] = 0 - j;
}
pd_y[i][j] = 1. - pu_y[i][j];
}

return 1;
}

static int lecture_tr()
{
    int i;
    char ligne[30];
    char *pligne;
    double p, tt_value;

```

```
FILE *Entrees;

Entrees = fopen(init_tr, "r");

if (Entrees == NULL)
{
    printf("Le FICHIER N'A PU ETRE OUVERT. VERIFIER LE CHEMIN\ n");
}

/* i is the number of libe that has been read */
i = 0;
pligne = ligne;
Pm = (double *)malloc(200 * sizeof(double));
tm = (double *)malloc(200 * sizeof(double));

while (1)
{
    pligne = fgets(ligne, sizeof(ligne), Entrees);
    if (pligne == NULL) break;
    else
    {
        sscanf(pligne, "%lf t=%lf", &p, &tt_value);
        /* The line read must be written "0.943290 t=0.5" where 0.943290 is a
        Pm[i] = p; /*save the price of the zero coupon*/
        tm[i] = tt_value; /*save the corresponding time*/
        i++;
    }
}

fclose(Entrees);

return i;
}

static void interpolate(int n_price, int imax, double *t)
{
    int i, iF, j;

    n_price--;

    i = 0;
```

```

while (t[i] <= tm[1])
{
    initial_yield[i] = (tm[1] - t[i]) / tm[1] + t[i] * Pm[1] / tm[1];
    i++;
}

for (j = 0; j < n_price; j++)
{
    while (t[i] < tm[j + 1] && i <= imax + 1)
    {
        initial_yield[i] = (tm[j + 1] - t[i]) / (tm[j + 1] - tm[j]) * Pm[j] +
        i++;
    }
}

if (t[i] > tm[n_price] && i <= imax + 1)
{
    for (iF = i ; iF <= imax ; iF++)
    {
        initial_yield[iF] = Pm[n_price] + (Pm[n_price] - Pm[n_price - 1]) / (t
    }
}
}

/*Calibration of the tree consistent with dynamic of the Hull-White Process*/
static int calibration_bond(int flat_flag, double tt, double r0, double omega, i
{
    double sum;
    int i, j, jj, n_price;
    double dt;

    dt = tt / (double)Nt;

    /*Initialilise Yield Curve*/
    if (flat_flag == 0)
    {
        for (i = 0; i <= Nt + 1; i++)
            initial_yield[i] = r0;
    }
}

```

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else
{
    double *t_vect;
    t_vect = (double *)malloc((Nt + 3) * sizeof(double));

    for (i = 0; i <= Nt + 2; i++)
        t_vect[i] = i * dt;
    n_price = lecture_tr();
    /* We search in initialyield.dat the biggest value before time T */
    if (tt > tm[n_price - 1])
    {
        printf("\ nError : time bigger than the last time value entered in ini
    }
    interpolate(n_price, Nt, t_vect);

    free(tm);
    free(Pm);
    free(t_vect);
}

for (i = 0; i <= Nt + 1; i++)
{
    if (flat_flag == 0)
    {
        Pc[i] = exp(-initial_yield[i] * i * dt);
    }
    else
    {
        Pc[i] = initial_yield[i];
    }
}

/*Initalise first node*/
Q[0][0] = 1.;

/*Evolve tree for the x=ln r*/
for (i = 0; i <= Nt; i++)
{
    /*Update pure security prices*/
    if (i > 0)
        for (j = 0; j <= i; j++)

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    {
        sum = 0.;

        for (jj = 0; jj <= i - 1; jj++)
        {
            if (jj + y_up[i - 1][jj] == j)
                sum += Q[i - 1][jj] * pu_y[i - 1][jj] * discount[i - 1][jj];
            if (jj + y_down[i - 1][jj] == j)
                sum += Q[i - 1][jj] * pd_y[i - 1][jj] * discount[i - 1][jj];
        }

        Q[i][j] = sum;
    }

    /*Compute shift a[i]*/
    if (i == 0)
        shift[0] = -log(Pc[1]) / dt;
    else
    {
        sum = 0.;
        for (j = 0; j <= i; j++)
            sum += Q[i][j] * exp(-omega * y[i][j] * dt);

        shift[i] = (log(sum) - log(Pc[i + 1])) / dt;
    }

    /*Compute x,r and discount factor d*/
    for (j = 0; j <= i; j++)
    {
        r[i][j] = omega * y[i][j] + shift[i];
        discount[i][j] = exp(-r[i][j] * dt);
    }
}

return 1;
}

/*Compute Price Option*/
int Mc_HybridTree_HesHw(double s0, NumFunc_1 *p, double tt, double divid, int
{

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double price_sample, mean_price, var_price;
int init_mc, ipath, i, k1, k2;
int simulation_dim;
double alpha, z_alpha;
double pterror_price;
double int_r, vol, interest_rate, y_s;
double dt, sqrt_dt;
double g1, w_t_1;
double Yt, St;
double rho3;
double new_vol, new_y_s;
double mu_z;
double sigma_z;

init_tr = curve;

if ((fabs(rhorv) > 0))
    return UNTREATED_CASE;

if (SQR(rhoSv) + SQR(rhoSr) >= 1.)
    return UNTREATED_CASE;

/*Memory Allocation*/
if (memory_allocation(Nt) != OK) return FAIL;

//Tree construction for r
tree_r(tt, r0, kappa, omega, Nt);
calibration_bond(flat_flag, tt, r0, omega, Nt);

//Tree construction for v
tree_v(tt, v02, kappa2, theta2, omega2, Nt);

/* Value to construct the confidence interval */
alpha= (1.- confidence)/2.;
z_alpha=pnl_inv_cdfnor(1.- alpha);

/*Initialisation*/
mean_price= 0.0;
var_price= 0.0;

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dt=tt/(double)Nt;
sqrt_dt=sqrt(dt);
/* Test after initialization for the generator */
simulation_dim =Nt;

/* MC sampling */
init_mc = pnl_rand_init(generator, simulation_dim, N_MC);
rho3=sqrt(1-SQR(rhoSv)-SQR(rhoSr));
for(ipath= 1;ipath<=N_MC;ipath++)
{
    vol=V[0][0];
    interest_rate=r[0][0];
    y_s=y[0][0];

    Yt=log(s0);
    k1=0;
    k2=0;
    int_r=0;
    for(i=0;i<Nt;i++)
    {
        g1=pnl_rand_normal(generator);//V
        w_t_1=sqrt_dt*g1;//V
        interest_rate=r[i][k1];

        //Simulate V
        if(pnl_rand_uni(generator)<pu_f[i][k2])
            k2+=f_up[i][k2];
        else
            k2+=f_down[i][k2];

        new_vol=V[i+1][k2];

        //Simulate r and y
        if(pnl_rand_uni(generator)<pu_y[i][k1])
            k1+=y_up[i][k1];
        else
            k1+=y_down[i][k1];

        new_y_s=y[i+1][k1];

        mu_z=interest_rate-divid-0.5*vol-rhoSv/omega2*kappa2*(theta2-vol)+sqrt(vol)*rh

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    sigma_z=rho3*sqrt(vol);

    Yt+=mu_z*dt+sigma_z*w_t_1+rhoSv/omega2*(new_vol-vol)+rhoSr*sqrt(vol)*(new_y_s-

    St=exp(Yt);

    y_s=new_y_s;
    vol=new_vol;

    int_r+=interest_rate;
}

price_sample=exp(-int_r*dt)*(p->Compute)(p->Par,St);

/* Sum */
mean_price+=price_sample;

/* Sum of squares */
var_price+= SQR(price_sample);
}

*ptprice=(mean_price/(double)N_MC);
pterror_price= sqrt(var_price/(double)N_MC-SQR(*ptprice))/sqrt((double)N_MC-1)

/* Price Confidence Interval */
*inf_price= *ptprice - z_alpha*(pterror_price);
*sup_price= *ptprice + z_alpha*(pterror_price);

/*Memory Disallocation*/
free_memory(Nt);

return OK;
}

int CALC(MC_HybridTree)(void *Opt, void *Mod, PricingMethod *Met)
{
    TYPEOPT *ptOpt = (TYPEOPT *)Opt;
    TYPEMOD *ptMod = (TYPEMOD *)Mod;
    double divid;

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divid = ptMod->divid.Val.V_DOUBLE;

return Mc_HybridTree_HesHw(ptMod->S0.Val.V_PDOUBLE,
                           ptOpt->PayOff.Val.V_NUMFUNC_1,
                           ptOpt->Maturity.Val.V_DATE - ptMod->T.Val.V_DATE, d
                           ptMod->flat_flag.Val.V_INT,
                           MOD(GetYield)(ptMod),
                           MOD(GetCurve)(ptMod),
                           ptMod->kr.Val.V_PDOUBLE,
                           ptMod->Sigmar.Val.V_PDOUBLE,
                           ptMod->V0.Val.V_PDOUBLE
                           , ptMod->kV.Val.V_PDOUBLE,
                           ptMod->thetaV.Val.V_PDOUBLE,
                           ptMod->SigmaV.Val.V_PDOUBLE,
                           ptMod->RhoSr.Val.V_PDOUBLE,
                           ptMod->RhoSV.Val.V_PDOUBLE,
                           ptMod->RhorV.Val.V_PDOUBLE,
                           Met->Par[0].Val.V_PINT,
                           Met->Par[1].Val.V_PINT,
                           Met->Par[2].Val.V_ENUM.value,
                           Met->Par[3].Val.V_PDOUBLE,
                           &(Met->Res[0].Val.V_DOUBLE), &(Met->Res[1].Val.V_DO
}

static int CHK_OPT(MC_HybridTree)(void *Opt, void *Mod)
{
    if ((strcmp(((Option *)Opt)->Name, "CallEuro") == 0) || (strcmp(((Option *)Opt
        return OK;
    return WRONG;
}
#endif //PremiaCurrentVersion

static int MET(Init)(PricingMethod *Met, Option *Opt)
{
    if (Met->init == 0)
    {
        Met->init = 1;
        Met->HelpFilenameHint = "mc_hybridtree_heshw";
        Met->Par[0].Val.V_INT = 300;
        Met->Par[1].Val.V_INT = 100000;
        Met->Par[2].Val.V_ENUM.value = 0;

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        Met->Par[2].Val.V_ENUM.members = &PremiaEnumMCRNGs;
        Met->Par[3].Val.V_DOUBLE = 0.95;
    }

    return OK;
}

PricingMethod MET(MC_HybridTree) =
{
    "MC_HybridTree",
    { {"N steps time", INT, {100}, ALLOW},
      {"N Iterations", INT, {100}, ALLOW},
{"RandomGenerator", ENUM, {100}, ALLOW},
      {"Confidence Value", DOUBLE, {100}, ALLOW},
      {" ", PREMIA_NULLTYPE, {0}, FORBID}
    },
    CALC(MC_HybridTree),
    { {"Price", DOUBLE, {100}, FORBID},
{"Inf Price", DOUBLE, {100}, FORBID},
      {"Sup Price", DOUBLE, {100}, FORBID} ,
      {" ", PREMIA_NULLTYPE, {0}, FORBID}
    },
    CHK_OPT(MC_HybridTree),
    CHK_ok,
    MET(Init)
};

```