

[Help](#)

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#include "cir1d_std.h"
#include "enums.h"

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion < (2009+2) //The "#els
static int CHK_OPT(MC_TEICHMANNBAYER)(void *Opt, void *Mod)
{
    return NONACTIVE;
}
int CALC(MC_TEICHMANNBAYER)(void *Opt, void *Mod, PricingMethod *Met)
{
    return AVAILABLE_IN_FULL_PREMIA;
}
#else

/* linear uniform interpolation of [0,T] of size N*/
/* return value = dt*/
static double linspace1(double T0, double T1, int N, double *t)
{
    double dt;
    int i;

    dt = (T1 - T0) / (double)(N - 1);
    t[0] = T0;
    for (i = 1; i < N; i++)
        t[i] = t[i - 1] + dt;
    return dt;
}
/* linear interpolation using stepsize dt; return T */
static double linspace2(double dt, int N, double *t)
{
    double T = dt * (double)(N - 1);
    int i;
    t[0] = 0.0;
    for (i = 1; i < N; i++)
        t[i] = t[i - 1] + dt;
    return T;
}
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/* extrapolate a CIR-HJM-forward rate curve from a short rate */
/* l is assumed to be the length of x */
static void CIR2HJM(double r0, double kappa, double theta, double sigma, double
{
    double g0, g1, G1;
    int i;
    for (i = 0; i < l; i++)
    {
        G1 = 2.0 * (exp(gamma_tb * x[i]) - 1.0) / ((gamma_tb + kappa) * (exp(gamma
        g0 = kappa * theta * G1;
        g1 = 4.0 * (gamma_tb * gamma_tb) * exp(gamma_tb * x[i]) / (((gamma_tb + ka
        r[i] = g0 + r0 * g1;
    }
}

/* Generate an Nxd-array of iid. Bernoullis with p = 0.5 */
/* actually, it would be enough to consider boolean variables here */
static void GenBernoulli1(int *J, int N, int generator)
{
    int i;
    for (i = 0; i < N; i++)
        if (pnl_rand_uni(generator) < 0.5)
            J[i] = 0;
        else J[i] = 1;
}

/* generate a vector of "brownian increments" given the multi-index J */
static void omegadot1(int N, double dt, int NCub, const int *J, int n, double *d
{
    int i, k;
    double tempd1 = sqrt(dt) / sqrt((double)(n));
    for (i = 0; i < (NCub - 1); i++)
    {
        for (k = 0; k < n; k++)
            dB[i * n + k] = (J[i] == 0) ? tempd1 : (- tempd1);
    }
    for (k = (n * (NCub - 1)); k < N; k++)
        dB[k] = (J[NCub - 1] == 0) ? tempd1 : (-tempd1);
}

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/* apply the shift semi-group */
/* i_shift is the integer part of the shift in terms of dx-units, r_shift
   the remainder */
static double Shift(const double *r, const double *x, double dx, double dt, int
{
    /*double ret;*/
    if (k < m - i_shift - 1)
        return (1.0 - r_shift) * r[k + i_shift] + r_shift * r[k + i_shift + 1];
    else
        return r[m - 1];
}

/* the vector field alpha0 */
static double alpha0(const double *r, double kappa, double theta, double sigma,
{
    double g1, G1;
    G1 = 2.0 * (expg - 1.0) / ((gamma_tb + kappa) * (expg - 1.0) + 2.0 * gamma_tb)
    g1 = 4.0 * (gamma_tb * gamma_tb) * expg / (((gamma_tb + kappa) * expg + gamma_
    return (sigma * sigma) * (g1) * (r[0] * (G1) - 0.25);
}

/* the volatility vector field(s) */
double HJMSigma(const double *r, double kappa, double theta, double sigma, doubl
{
    return sigma * sqrtr * (4.0 * (gamma * gamma) * expg / (((gamma + kappa) * exp
}

/* value P(0,T) of a zero coupon bond */
static double ZeroCB(const double *r, const double *x, double dx, double T)
{
    int Tx = ceil(T / dx);    /* index of T in the x-grid */
    double integ = 0.0;
    int i;
    for (i = 0; i < Tx; i++)
        integ += 0.5 * (r[i] + r[i + 1]) * dx;
    return exp(- integ);
}

/* compute the empirical mean value of a vector */
static double mean(const double *X, int M)
{

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double ret = 0.0;
int i;
for (i = 0; i < M; i++)
    ret += X[i];
ret = ret / (double)(M);
return ret;
}
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/* compute the empirical standard deviation of a vector */
static double stdev(const double *X, int M)
{
    double mu = mean(X, M);
    double ret = 0.0;
    int i;
    for (i = 0; i < M; i++)
        ret += X[i] * X[i];
    ret = ret / (double)(M);
    ret = sqrt(ret - mu * mu);
    return ret;
}
```

```
/* n number of time intervals on each cubature interval*/
/* N number of time intervals*/
/* m number of space intervals*/
/* M number of paths for Monte-Carlo simulation*/
static int mc_teichmannbayer(double r0, double kappa, double t0, double sigma, d
{
    double gamma_tb = 0;
    int NCub;
    double *t;
    double dt = 0;
    double dx = 0;
    int mAct = 0;
    double *x;
    double r_shift = 0;
    int i_shift = 0;
    int *J;
    double *r;
    double *rp, *rm, *rpc, *rmc;
    double *res, *dB;
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double Bp, Bm; /* savings account */
double expg, sqrtrm, sqrtrp; /* auxiliary variable*/
int i, j;
int ii, k_bis;
double zerop = 0;
double zerom = 0;

gamma_tb = sqrt((kappa * kappa) + 2.0 * (sigma * sigma));
pnl_rand_init(generator, 1, M);

/* first generate the time and space grids */
if (L % n == 0)
    NCub = L / n;
else
    NCub = L / n + 1;
/* generate the time grid */
t = malloc((L + 1) * sizeof(double));
dt = linspace1(t0, T_option, L + 1, t);
/* generate the spacegrid */
dx = (T_bond - T_option) / (double)(k);
mAct = (int)(T_option / dx) + k + (int)(L * (dt / dx)) + 1;
x = malloc((mAct + 1) * sizeof(double));
dt = linspace1(t0, T_option, L + 1, t);
linspace2(dx, mAct + 1, x);
/* for the shift semigroup, express dt in temrs of dx:
    dt = i_shift * dx + r_shift * dx */
r_shift = dt / dx;
i_shift = (int)(r_shift);
r_shift = r_shift - i_shift;

/* J describes one cubature path */
J = malloc((NCub) * sizeof(int));

/* generate the initial forward rate curve */
r = malloc((mAct + 1) * sizeof(double)); /* saves initial forward rate curve */
CIR2HJM(r0, kappa, theta, sigma, gamma_tb, x, mAct + 1, r);

rp = malloc((mAct + 1) * sizeof(double));
rm = malloc((mAct + 1) * sizeof(double));
rpc = malloc((mAct + 1) * sizeof(double));
rmc = malloc((mAct + 1) * sizeof(double));

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/* the path-wise discounted payoff */
res = malloc((M) * sizeof(double));

/* the "brownian" increments (i.e. the cubature derivatives) */
dB = malloc((L) * sizeof(double));

/* now iterate through all paths for the MC-simulation*/
for (j = 0; j < M; j++)
{
    /* re-initialize r and B */
    GenBernoulli1(J, NCub, generator); /* generate J */

    for (i = 0; i < mAct + 1; i++)
    {
        rp[i] = r[i];
        rm[i] = r[i];
    }

    Bp = 1.0;
    Bm = 1.0;

    /* generate dB */
    omegadot1(L, dt, NCub, J, n, dB);

    /* iterate through the time grid */
    for (i = 0; i < L; i++)
    {
        sqrtrp = (rp[0] > 0.0) ? sqrt(rp[0]) : 0.0;
        sqrtrm = (rm[0] > 0.0) ? sqrt(rm[0]) : 0.0;
        Bp += Bp * rp[0] * dt;
        Bm += Bm * rm[0] * dt;
        for (ii = 0; ii < mAct + 1; ii++)
        {
            rpc[ii] = rp[ii];
            rmc[ii] = rm[ii];
        }

        /* iterate through the space grid */
        for (k_bis = 0; k_bis <= mAct; k_bis++)
        {

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        expg = exp(gamma_tb * x[k_bis]);
        rp[k_bis] = Shift(rpc, x, dx, dt, mAct + 1, k_bis, i_shift, r_shif
        rp[k_bis] += HJMSigma(rpc, kappa, theta, sigma, gamma_tb, x, mAct
        rm[k_bis] = Shift(rmc, x, dx, dt, mAct + 1, k_bis, i_shift, r_shif
        rm[k_bis] -= HJMSigma(rmc, kappa, theta, sigma, gamma_tb, x, mAct
    }
}
/* compute the discounted payoff for this particular path */
zerop = ZeroCB(rp, x, dx, T_bond - T_option);
zerom = ZeroCB(rm, x, dx, T_bond - T_option);

    res[j] = 0.5 * ((p->Compute)(p->Par, zerop) / Bp + (p->Compute)(p->Par, ze
}
/*Price*/
*price = mean(res, M);

/*Estimate Error*/
*error = 1.65 * stdev(res, M) / sqrt((double)(M));

/* free memory again */
free(t);
free(x);
free(J);
free(r);
free(rp);
free(rpc);
free(rm);
free(rmc);
free(res);
free(dB);

return OK;
}

int CALC(MC_TEICHMANNBAYER)(void *Opt, void *Mod, PricingMethod *Met)
{
    TYPEOPT *ptOpt = (TYPEOPT *)Opt;
    TYPEMOD *ptMod = (TYPEMOD *)Mod;

    return mc_teichmannbayer(ptMod->r0.Val.V_PDOUBLE, ptMod->k.Val.V_DOUBLE, ptMod
        ptMod->theta.Val.V_PDOUBLE, ptOpt->BMaturity.Val.V_DA

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}

static int CHK_OPT(MC_TEICHMANNBAYER)(void *Opt, void *Mod)
{
    if ((strcmp(((Option *)Opt)->Name, "ZeroCouponCallBondEuro") == 0) || (strcmp(
        return OK;
    else
        return WRONG;
}

#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met, Option *Opt)
{
    if (Met->init == 0)
    {
        Met->init = 1;
        Met->Par[0].Val.V_ENUM.value = 0;
        Met->Par[0].Val.V_ENUM.members = &PremiaEnumMCRNGs;
        Met->Par[1].Val.V_PINT = 20;
        Met->Par[2].Val.V_PINT = 400;
        Met->Par[3].Val.V_PINT = 10;
        Met->Par[4].Val.V_PINT = 20;
    }

    return OK;
}

PricingMethod MET(MC_TEICHMANNBAYER) =
{
    "MC_TEICHMANNBAYER",

    { {"RandomGenerator", ENUM, {100}, ALLOW},
      {"Number of time intervals on each cubature interval", INT, {100}, ALLOW},
      {"Number of time intervals", INT, {100}, ALLOW},
      {"Number of space intervals*", INT, {100}, ALLOW},
      {"Number of paths for Monte-Carlo simulation", PINT, {100}, ALLOW},
      {" ", PREMIA_NULLTYPE, {0}, FORBID}
    },
    CALC(MC_TEICHMANNBAYER),
    {"Price", DOUBLE, {100}, FORBID}, {"MC Error", DOUBLE, {100}, FORBID} , {" ",
    CHK_OPT(MC_TEICHMANNBAYER),

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    CHK_ok,  
    MET(Init)  
} ;
```