

[Help](#)

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#include "cir2d_std.h"
#include "enums.h"

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion < (2009+2) //The "#els
static int CHK_OPT(MC_CIR2D_TEICHMANNBAYER)(void *Opt, void *Mod)
{
    return NONACTIVE;
}
int CALC(MC_CIR2D_TEICHMANNBAYER)(void *Opt, void *Mod, PricingMethod *Met)
{
    return AVAILABLE_IN_FULL_PREMIA;
}
#else
/* linear uniform interpolation of [0,T] of size N*/
/* return value = dt*/
static double linspace1(double T0, double T1, int N, double *t)
{
    double dt;
    int i;

    dt = (T1 - T0) / (double)(N - 1);
    t[0] = T0;
    for (i = 1; i < N; i++)
        t[i] = t[i - 1] + dt;
    return dt;
}
/* linear interpolation using stepsize dt; return T */
static double linspace2(double dt, int N, double *t)
{
    double T = dt * (double)(N - 1);
    int i;
    t[0] = 0.0;
    for (i = 1; i < N; i++)
        t[i] = t[i - 1] + dt;
    return T;
}

/* extrapolate a CIR-HJM-forward rate curve from a short rate */

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/* l is assumed to be the length of x */
static void CIR2HJM(double r0, double kappa, double theta, double sigma, double
{
    double g0, g1, G1;
    int i;
    for (i = 0; i < l; i++)
    {
        G1 = 2.0 * (exp(gamma_tb * x[i]) - 1.0) / ((gamma_tb + kappa) * (exp(gamma
        g0 = kappa * theta * G1;
        g1 = 4.0 * (gamma_tb * gamma_tb) * exp(gamma_tb * x[i]) / (((gamma_tb + ka
        r[i] = g0 + r0 * g1;
    }
}

/* very bad random number generator */
static void GenBernoulli2(int **J, int N, int generator)
{
    int i, j;
    for (i = 0; i < N; i++)
        for (j = 0; j < 2; j++)
            if (pnl_rand_uni(generator) < 0.5)
                J[i][j] = 0;
            else J[i][j] = 1;
}

static void CopyVect(const double *orig, double *dest, int N)
{
    int i;
    for (i = 0; i < N; i++)
        dest[i] = orig[i];
}

static void omegadot2(int N, double dt, int NCub, int **J, int n, double **dB)
{
    double tempd1 = sqrt(dt) / sqrt((double)(n));
    int i, k;
    for (i = 0; i < (NCub - 1); i++)
    {
        for (k = 0; k < n; k++)
        {

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        dB[i * n + k][0] = (J[i][0] == 0) ? tempd1 : (- tempd1);
        dB[i * n + k][1] = (J[i][1] == 0) ? tempd1 : (- tempd1);
    }
}
for (k = (n * (NCub - 1)); k < N; k++)
{
    dB[k][0] = (J[NCub - 1][0] == 0) ? tempd1 : (-tempd1);
    dB[k][1] = (J[NCub - 1][1] == 0) ? tempd1 : (-tempd1);
}
}

static double Shift(const double *r, const double *x, double dx, double dt, int
{
    /*double ret;*/
    if (k < m - i_shift - 1)
        return (1.0 - r_shift) * r[k + i_shift] + r_shift * r[k + i_shift + 1];
    else
        return r[m - 1];
}

static double alpha0(const double *r, double kappa, double theta, double sigma,
{
    double g1, G1;
    G1 = 2.0 * (expg - 1.0) / ((gamma + kappa) * (expg - 1.0) + 2.0 * gamma);
    g1 = 4.0 * (gamma * gamma) * expg / (((gamma + kappa) * expg + gamma - kappa)
    return (sigma * sigma) * (g1) * (r[0] * (G1) - 0.25);
}

static double HJMSigma(const double *r, double kappa, double theta, double sigma,
{
    return sigma * sqrtr * (4.0 * (gamma * gamma) * expg / (((gamma + kappa) * expg
}

/* value P(0,T) of a zero coupon bond */
static double ZeroCB(const double *r, const double *x, double dx, double T)
{
    int Tx = ceil(T / dx);    /* index of T in the x-grid */
    double integ = 0.0;
    int i;
    for (i = 0; i < Tx; i++)

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    integ += 0.5 * (r[i] + r[i + 1]) * dx;
    return exp(- integ);
}
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/* compute the empirical mean value of a vector */
static double mean(const double *X, int M)
{
    double ret = 0.0;
    int i;
    for (i = 0; i < M; i++)
        ret += X[i];
    ret = ret / (double)(M);
    return ret;
}
```

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/* compute the empirical standard deviation of a vector */
static double stdev(const double *X, int M)
{
    double mu = mean(X, M);
    double ret = 0.0;
    int i;
    for (i = 0; i < M; i++)
        ret += X[i] * X[i];
    ret = ret / (double)(M);
    ret = sqrt(ret - mu * mu);
    return ret;
}
```

```
/* n number of time intervals on each cubature interval*/
/* N number of time intervals*/
/* m number of space intervals*/
/* M number of paths for Monte-Carlo simulation*/
static int mc_cir2d_teichmannbayer(double x01, double x02, double k1, double k2,
{
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    double delta;
    double kappa[2], theta[2], sigma[2], r0[2];
    double gamma[2];
    int NCub;
```

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double *t, dt, *x, dx, r_shift;
int mAct, i_shift;
int i;
int **J;
double *r1, *r2;
double *rp, *rm, *rp1, *rm1, *rpc1, *rmc1, *rp2, *rm2, *rpc2, *rmc2;
double *res;
double Bp, Bm; /* savings account */
double expg1, expg2, sqrtrm1, sqrtrp1, sqrtrm2, sqrtrp2; /* auxiliary variabl
int j;
int k_bis;
double zerop, zerom;
double **dB;

pnl_rand_init(generator, 1, M);

kappa[0] = k1;
kappa[1] = k2;
theta[0] = theta1;
theta[1] = theta2;
sigma[0] = sigma1;
sigma[1] = sigma2;
r0[0] = x01;
r0[1] = x02;
delta = shift;
gamma[0] = sqrt((kappa[0] * kappa[0]) + 2.0 * (sigma[0] * sigma[0]));
gamma[1] = sqrt((kappa[1] * kappa[1]) + 2.0 * (sigma[1] * sigma[1]));

if (L % n == 0)
    NCub = L / n;
else
    NCub = L / n + 1;

/* generate the time grid */
t = malloc((L + 1) * sizeof(double));
dt = linspace1(t0, T_option, L + 1, t);
/* generate the spacegrid */
dx = (T_bond - T_option) / (double)(k);
mAct = (int)(T_option / dx) + k + (int)(L * (dt / dx)) + 1;

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x = malloc((mAct + 1) * sizeof(double));
dt = linspace1(t0, T_option, L + 1, t);
linspace2(dx, mAct + 1, x);
/* for the shift semigroup, express dt in temrs of dx:
  dt = i_shift * dx + r_shift * dx */
r_shift = dt / dx;
i_shift = (int)(r_shift);
r_shift = r_shift - i_shift;

/* J describes one cubature path */
J = (int **)calloc(NCub, sizeof(int *));
for (i = 0; i < NCub; i++)
    J[i] = (int *)calloc(2, sizeof(int));

/* generate the initial forward rate curve */
r1 = malloc((mAct + 1) * sizeof(double));/* saves initial
                                           * forward rate curve
*/
r2 = malloc((mAct + 1) * sizeof(double)); /* saves initial forward rate curve

CIR2HJM(r0[0], kappa[0], theta[0], sigma[0], gamma[0], x, mAct + 1, r1);
CIR2HJM(r0[1], kappa[1], theta[1], sigma[1], gamma[1], x, mAct + 1, r2);

rp = malloc((mAct + 1) * sizeof(double));
rm = malloc((mAct + 1) * sizeof(double));
rp1 = malloc((mAct + 1) * sizeof(double));
rm1 = malloc((mAct + 1) * sizeof(double));
rpc1 = malloc((mAct + 1) * sizeof(double));
rmc1 = malloc((mAct + 1) * sizeof(double));
rp2 = malloc((mAct + 1) * sizeof(double));
rm2 = malloc((mAct + 1) * sizeof(double));
rpc2 = malloc((mAct + 1) * sizeof(double));
rmc2 = malloc((mAct + 1) * sizeof(double));

/* the path-wise discounted payoff */
res = malloc((M) * sizeof(double));

/* the "brownian" increments (i.e. the cubature derivatives) */
dB = (double **)calloc(L, sizeof(double *));
for (i = 0; i < L; i++)

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    dB[i] = (double *)calloc(2, sizeof(double));

/* now iterate through all paths for the MC-simulation*/
for (j = 0; j < M; j++)
{
    /* re-initialize r and B */
    GenBernoulli2(J, NCub, generator); /* generate J */
    CopyVect(r1, rp1, mAct + 1);
    CopyVect(r1, rm1, mAct + 1);
    CopyVect(r2, rp2, mAct + 1);
    CopyVect(r2, rm2, mAct + 1);
    Bp = 1.0;
    Bm = 1.0;

    /* generate dB */
    omegadot2(L, dt, NCub, J, n, dB);

    /* iterate through the time grid */

    for (i = 0; i < L; i++)
    {
        sqrtrp1 = (rp1[0] > 0.0) ? sqrt(rp1[0]) : 0.0;
        sqrtrm1 = (rm1[0] > 0.0) ? sqrt(rm1[0]) : 0.0;
        sqrtrp2 = (rp2[0] > 0.0) ? sqrt(rp2[0]) : 0.0;
        sqrtrm2 = (rm2[0] > 0.0) ? sqrt(rm2[0]) : 0.0;
        Bp += Bp * (delta + rp1[0] + rp2[0]) * dt;
        Bm += Bm * (delta + rm1[0] + rm2[0]) * dt;
        CopyVect(rp1, rpc1, mAct + 1);
        CopyVect(rm1, rmc1, mAct + 1);
        CopyVect(rp2, rpc2, mAct + 1);
        CopyVect(rm2, rmc2, mAct + 1);
        /* iterate through the space grid */
        for (k_bis = 0; k_bis <= mAct; k_bis++)
        {
            expg1 = exp(gamma[0] * x[k_bis]);
            expg2 = exp(gamma[1] * x[k_bis]);
            rp1[k_bis] = Shift(rpc1, x, dx, dt, mAct + 1, k_bis, i_shift, r_sh
            rp1[k_bis] += HJMSigma(rpc1, kappa[0], theta[0], sigma[0], gamma[0]
            rm1[k_bis] = Shift(rmc1, x, dx, dt, mAct + 1, k_bis, i_shift, r_sh
            rm1[k_bis] -= HJMSigma(rmc1, kappa[0], theta[0], sigma[0], gamma[0]
            rp2[k_bis] = Shift(rpc2, x, dx, dt, mAct + 1, k_bis, i_shift, r_sh

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        rp2[k_bis] += HJMSigma(rpc2, kappa[1], theta[1], sigma[1], gamma[1]
        rm2[k_bis] = Shift(rmc2, x, dx, dt, mAct + 1, k_bis, i_shift, r_sh
        rm2[k_bis] -= HJMSigma(rmc2, kappa[1], theta[1], sigma[1], gamma[1]
    }
}

/* Now combine the three components, delta, r1, r2 into the forward rate *
/* curve r. */
for (k_bis = 0; k_bis <= mAct; k_bis++)
{
    rp[k_bis] = delta + rp1[k_bis] + rp2[k_bis];
    rm[k_bis] = delta + rm1[k_bis] + rm2[k_bis];
}
/* compute the discounted payoff for this particular path */
/* compute the discounted payoff for this particular path */
zerop = ZeroCB(rp, x, dx, T_bond - T_option);
zerom = ZeroCB(rm, x, dx, T_bond - T_option);

res[j] = 0.5 * ((p->Compute)(p->Par, zerop) / Bp + (p->Compute)(p->Par, ze
}

*price = mean(res, M);
*error = 1.65 * stdev(res, M) / sqrt((double)(M));

/* free memory */
free(t);
free(x);
free(r1);
free(r2);
free(rp);
free(rm);
free(rp1);
free(rpc1);
free(rm1);
free(rmc1);
free(rp2);
free(rpc2);
free(rm2);
free(rmc2);
free(res);

for (i = 0; i < L; i++)

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        free(dB[i]);
    free(dB);

    for (i = 0; i < NCub; i++)
        free(J[i]);
    free(J);

    return OK;
}

int CALC(MC_CIR2D_TEICHMANNBAYER)(void *Opt, void *Mod, PricingMethod *Met)
{
    TYPEOPT *ptOpt = (TYPEOPT *)Opt;
    TYPEMOD *ptMod = (TYPEMOD *)Mod;

    return mc_cir2d_teichmannbayer(ptMod->x01.Val.V_PDDOUBLE, ptMod->x02.Val.V_PDDOUBLE);
}

static int CHK_OPT(MC_CIR2D_TEICHMANNBAYER)(void *Opt, void *Mod)
{
    if ((strcmp(((Option *)Opt)->Name, "ZeroCouponCallBondEuro") == 0) || (strcmp(
        return OK;
    else
        return WRONG;
}

#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met, Option *Opt)
{
    if (Met->init == 0)
    {
        Met->init = 1;
        Met->Par[0].Val.V_ENUM.value = 0;
        Met->Par[0].Val.V_ENUM.members = &PremiaEnumMCRNGs;
        Met->Par[1].Val.V_PINT = 20;
        Met->Par[2].Val.V_PINT = 400;
        Met->Par[3].Val.V_PINT = 10;
        Met->Par[4].Val.V_PINT = 20;
    }
}

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    return OK;
}

PricingMethod MET(MC_CIR2D_TEICHMANNBAYER) =
{
    "MC_CIR2D_TEICHMANNBAYER",

    { {"RandomGenerator", ENUM, {100}, ALLOW},
      {"Number of time intervals on each cubature interval", INT, {100}, ALLOW},
      {"Number of time intervals", INT, {100}, ALLOW},
      {"Number of space intervals*", INT, {100}, ALLOW},
      {"Number of paths for Monte-Carlo simulation", PINT, {100}, ALLOW},
      {" ", PREMIA_NULLTYPE, {0}, FORBID}
    },
    CALC(MC_CIR2D_TEICHMANNBAYER),
    {{"Price", DOUBLE, {100}, FORBID}, {"MC Error", DOUBLE, {100}, FORBID} , {" ",
    CHK_OPT(MC_CIR2D_TEICHMANNBAYER),
    CHK_ok,
    MET(Init)
} ;

```