

[Help](#)

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#include <stdlib.h>
#include "
href../../mod/bs2d/bs2d_std2d/bs2d_std2d_h_src.pdfbs2d_std2d.h"
#include "
href../../common/error_msg_h_src.pdferror_msg.h"
#include "
href../../common/enums_h_src.pdfenums.h"

static double *Q = NULL, *Weights = NULL, *Trans = NULL, *Price = NULL;
static double *Aux_Path = NULL, *Aux_Stock = NULL, *Aux_BS = NULL;
static double *Sigma = NULL;
static int *Path_Int = NULL;

static int RaQ_Allocation(int AL_T_Size, int BS_Dimension,
                          int OP_Exercice_Dates)
{
    if (Q == NULL)
        Q = malloc(AL_T_Size * OP_Exercice_Dates * BS_Dimension * sizeof(double));
    if (Q == NULL)
        return MEMORY_ALLOCATION_FAILURE;

    if (Trans == NULL)
        Trans = malloc(OP_Exercice_Dates * AL_T_Size * AL_T_Size * sizeof(double));
    if (Trans == NULL)
        return MEMORY_ALLOCATION_FAILURE;

    if (Weights == NULL)
        Weights = malloc(OP_Exercice_Dates * AL_T_Size * sizeof(double));
    if (Weights == NULL)
        return MEMORY_ALLOCATION_FAILURE;

    if (Price == NULL)
        Price = malloc(OP_Exercice_Dates * AL_T_Size * sizeof(double));
    if (Price == NULL)
        return MEMORY_ALLOCATION_FAILURE;

    if (Aux_Path == NULL)
        Aux_Path = malloc(OP_Exercice_Dates * BS_Dimension * sizeof(double));
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    if (Aux_Path == NULL)
        return MEMORY_ALLOCATION_FAILURE;

    if (Aux_Stock == NULL)
        Aux_Stock = malloc(BS_Dimension * sizeof(double));
    if (Aux_Stock == NULL)
        return MEMORY_ALLOCATION_FAILURE;

    if (Aux_BS == NULL)
        Aux_BS = malloc(BS_Dimension * sizeof(double));
    if (Aux_BS == NULL)
        return MEMORY_ALLOCATION_FAILURE;

    if (Sigma == NULL)
        Sigma = malloc(BS_Dimension * BS_Dimension * sizeof(double));
    if (Sigma == NULL)
        return MEMORY_ALLOCATION_FAILURE;

    if (Path_Int == NULL)
        Path_Int = malloc(OP_Exercice_Dates * sizeof(int));
    if (Path_Int == NULL)
        return MEMORY_ALLOCATION_FAILURE;

    return OK;
}

static void RaQ_Liberation()
{
    if (Q != NULL)
    {
        free(Q);
        Q = NULL;
    }
    if (Trans != NULL)
    {
        free(Trans);
        Trans = NULL;
    }
    if (Weights != NULL)
    {
        free(Weights);
    }
}

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        Weights = NULL;
    }
    if (Price != NULL)
    {
        free(Price);
        Price = NULL;
    }
    if (Aux_Path != NULL)
    {
        free(Aux_Path);
        Aux_Path = NULL;
    }
    if (Aux_Stock != NULL)
    {
        free(Aux_Stock);
        Aux_Stock = NULL;
    }

    if (Aux_BS != NULL)
    {
        free(Aux_BS);
        Aux_BS = NULL;
    }

    if (Sigma != NULL)
    {
        free(Sigma);
        Sigma = NULL;
    }
    if (Path_Int != NULL)
    {
        free(Path_Int);
        Path_Int = NULL;
    }
    return;
}

static int NearestCell(int Time, int AL_T_Size, long OP_EmBS_Di, int BS_Dimension)
{
    int j, k, l = 0;
    double min = DBL_MAX, aux, auxnorm;

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for (j = 0; j < AL_T_Size; j++)
{
    aux = 0;
    for (k = 0; k < BS_Dimension; k++)
    {
        auxnorm = Aux_Path[Time * BS_Dimension + k] -
            Q[(long)j * OP_EmBS_Di + Time * BS_Dimension + k];
        aux += auxnorm * auxnorm;
    }
    if (min > aux)
    {
        min = aux;
        l = j;
    }
}
return l;
}

static void ForwardPath(double *Path, double *Initial_Stock, int Initial_Time, i
{
    int i, j, k;
    double aux;
    double *SigmapjmBS_Dimensionpk;

    for (j = 0; j < BS_Dimension; j++) Path[Initial_Time * BS_Dimension + j] = Ini

    for (i = Initial_Time + 1; i < Initial_Time + Number_Dates; i++)
    {
        for (j = 0; j < BS_Dimension; j++)
        {
            Aux_Stock[j] = Sqrt_Step * pnl_rand_normal(generator);
        }
        SigmapjmBS_Dimensionpk = Sigma;

        for (j = 0; j < BS_Dimension; j++)
        {
            aux = 0.;
            for (k = 0; k <= j; k++)
            {
                aux += (*SigmapjmBS_Dimensionpk) * Aux_Stock[k];
                SigmapjmBS_Dimensionpk++;
            }
        }
    }
}

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        }
        SigmapjmBS_Dimensionpk += BS_Dimension - j - 1;
        aux -= Step * Aux_BS[j];
        Path[i * BS_Dimension + j] = Path[(i - 1) * BS_Dimension + j] * exp(aux);
    }
}

static double Discount(double Time, double BS_Interest_Rate)
{
    return exp(-BS_Interest_Rate * Time);
}

static void Init_Tesselations(long AL_MonteCarlo_Iterations, int AL_T_Size, int
{
    int i, j, k, Vimoins, Vi;
    long l;
    long OP_ExmBS_Di = (long)OP_Exercice_Dates * BS_Dimension;

    /* Random Quantizers */
    for (i = 0; i < AL_T_Size; i++)
        ForwardPath(Q + i * OP_Exercice_Dates * BS_Dimension, BS_Spot, 0, OP_Exercice_Dates,
                    generator, BS_Dimension, Step, Sqrt_Step);

    /* Weights and Transitions */
    for (i = 0; i < OP_Exercice_Dates; i++)
        for (j = 0; j < AL_T_Size; j++)
            Weights[i * AL_T_Size + j] = 0;

    for (i = 0; i < OP_Exercice_Dates; i++)
        for (j = 0; j < AL_T_Size; j++)
            for (k = 0; k < AL_T_Size; k++)
                Trans[i * AL_T_Size * AL_T_Size + j * AL_T_Size + k] = 0;

    for (l = 0; l < AL_MonteCarlo_Iterations - AL_T_Size; l++)
    {

        /*Black-Sholes Paths from time 0 to maturity*/
        ForwardPath(Aux_Path, BS_Spot, 0, OP_Exercice_Dates, generator, BS_Dimensi

        Vimoins = 0;

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        for (i = 1; i < OP_Exercice_Dates; i++)
        {
            Vi = NearestCell(i, AL_T_Size, OP_ExmBS_Di, BS_Dimension);
            Weights[i * AL_T_Size + Vi] += 1;
            Trans[i * AL_T_Size * AL_T_Size + Vimoins * AL_T_Size + Vi] += 1;
            Vimoins = Vi;
        }
    }
    Weights[0] = AL_MonteCarlo_Iterations - AL_T_Size;
    for (i = 1; i < OP_Exercice_Dates; i++)
        for (j = 0; j < AL_T_Size; j++)
            if (Weights[(i - 1)*AL_T_Size + j] > 0)
                for (k = 0; k < AL_T_Size; k++)
                    Trans[i * AL_T_Size * AL_T_Size + j * AL_T_Size + k] /= Weights[(i - 1) * AL_T_Size + j];
}

static void RaQ(double *PrixDir, long MC_Iterations, NumFunc_2 *p, int size, int BS_Dimension)
{
    int i, j, k, BS_Dimension = 2;
    long l;
    double step, Sqrt_Step, DiscountStep, aux, AL_BPrice, AL_FPrice;

    *PrixDir = 0.;
    step = t / (exercise_date_number - 1.);
    Sqrt_Step = sqrt(step);
    DiscountStep = exp(-r * step);

    /*Memory Allocation*/
    RaQ_Allocation(size, BS_Dimension, exercise_date_number);

    /*Black-Sholes initialization parameters*/
    Sigma[0] = sigma[0];
    Sigma[1] = sigma[1];
    Sigma[2] = sigma[2];
    Sigma[3] = sigma[3];

    Aux_BS[0] = 0.5 * (SQR(sigma[0]) + SQR(sigma[1])) - r + divid[0];
    Aux_BS[1] = 0.5 * (SQR(sigma[2]) + SQR(sigma[3])) - r + divid[1];
}

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/* Cells Weights and Transitions probabilities */
Init_Tesselations(MC_Iterations, size, exercise_date_number, generator, BS_Dimensions);

for (i = 0; i < size; i++)
    Price[(exercise_date_number - 1)*size + i] = 0;

/* Dynamical programming (backward price)*/
for (i = exercise_date_number - 2; i >= 1; i--)
{
    for (j = 0; j < size; j++)
    {
        aux = 0;

        /*Payoff control variate*/
        for (k = 0; k < size; k++)
        {
            aux += (Price[(i + 1) * size + k] + (p->Compute)(p->Par, *(Q + k *
                Trans[(i + 1) * size * size + j * size + k];
        }
        aux *= DiscountStep;
        aux -= (p->Compute)(p->Par, *(Q + j * exercise_date_number * BS_Dimensions));
        Price[i * size + j] = MAX(0., aux);
    }
}

aux = 0;
for (k = 0; k < size; k++)
    aux += (Price[size + k] + (p->Compute)(p->Par, *(Q + k * exercise_date_number * BS_Dimensions)));

/*Backward Price*/
aux *= DiscountStep;
if (!gj_flag)
    AL_BPrice = MAX((p->Compute)(p->Par, s_vector[0], s_vector[1]), aux);
else AL_BPrice = aux;

/* Forward price */
for (k = 0; k < size; k++)
{
    Price[k] = AL_BPrice - (p->Compute)(p->Par, s_vector[0], s_vector[1]);
}

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AL_FPrice = 0.0;
for (j = 0; j < size; j++)
{
    i = -1;
    do
    {
        i++;
    }
    while (0 < Price[i * size + j]);

    AL_FPrice += Discount((double)i * step, r) * (Price[i * size + j] +
        (p->Compute)(p->Par, *(Q + j * exercise_date_number * BS_Dime
    }

for (l = 0; l < MC_Iterations - size; l++)
{

    ForwardPath(Aux_Path, s_vector, 0, exercise_date_number, generator, BS_Dim
    Path_Int[0] = 0;
    for (i = 1; i < exercise_date_number; i++)
    {
        Path_Int[i] = NearestCell(i, size, exercise_date_number *
            BS_Dimension, BS_Dimension);
    }

    i = -1;
    do
    {
        i++;
    }
    while (0 < Price[i * size + Path_Int[i]]);
    AL_FPrice += Discount((double)i * step, r) * (Price[i * size + Path_Int[i]
        (p->Compute)(p->Par, *(Q + Path_Int[i] * exercise_date_number
    }

AL_FPrice /= (double)MC_Iterations;

/*Memory Disallocation*/
if (Fermeture)
    RaQ_Liberation();

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    /*Price=Forward Price*/
    *PrixDir = AL_FPrice;

    return;
}

static int MCRandomQuantization2D(double s1, double s2, NumFunc_2 *p, double t,
{

    double p1, p2, p3;
    int simulation_dim = 1, fermeture = 1, init_mc;
    double s_vector[2];
    double s_vector_plus1[2], s_vector_plus2[2];
    double sigma[4];
    double divid[2];

    /* Covariance Matrix */
    /* Coefficients of the matrix A such that A(tA)=Gamma */
    sigma[0] = sigma1;
    sigma[1] = 0.0;
    sigma[2] = rho * sigma2;
    sigma[3] = sigma2 * sqrt(1.0 - SQR(rho));

    /*Initialisation*/
    s_vector[0] = s1;
    s_vector[1] = s2;
    s_vector_plus1[0] = s1 * (1. + increment);
    s_vector_plus1[1] = s2;
    s_vector_plus2[0] = s1;
    s_vector_plus2[1] = s2 * (1. + increment);
    divid[0] = divid1;
    divid[1] = divid2;

    /*MC sampling*/
    init_mc = pnl_rand_init(generator, simulation_dim, N);

    /* Test after initialization for the generator */
    if (init_mc == OK)
    {

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/*Geske-Johnson Formulae*/
if (exercise_date_number == 0)
{
    RaQ(&p1, N, p, size_tesselation, fermeture, generator, 2, s_vector, t,
    RaQ(&p2, N, p, size_tesselation, fermeture, generator, 3, s_vector, t,
    RaQ(&p3, N, p, size_tesselation, fermeture, generator, 4, s_vector, t,
    *ptprice = p3 + 7. / 2.*(p3 - p2) - (p2 - p1) / 2.;
}
else
{
    RaQ(ptprice, N, p, size_tesselation, fermeture, generator, exercise_da
}

/*Delta*/
if (exercise_date_number == 0)
{
    RaQ(&p1, N, p, size_tesselation, fermeture, generator, 2, s_vector_plu
    RaQ(&p2, N, p, size_tesselation, fermeture, generator, 3, s_vector_plu
    RaQ(&p3, N, p, size_tesselation, fermeture, generator, 4, s_vector_plu

    *ptdelta1 = ((p3 + 7. / 2.*(p3 - p2) - (p2 - p1) / 2) - *ptprice) / (s

    RaQ(&p1, N, p, size_tesselation, fermeture, generator, 2, s_vector_plu
    RaQ(&p2, N, p, size_tesselation, fermeture, generator, 3, s_vector_plu
    RaQ(&p3, N, p, size_tesselation, fermeture, generator, 4, s_vector_plu
    *ptdelta2 = ((p3 + 7. / 2.*(p3 - p2) - (p2 - p1) / 2) - *ptprice) / (s
}
else
{
    RaQ(&p1, N, p, size_tesselation, fermeture, generator, exercise_date_n
    RaQ(&p2, N, p, size_tesselation, fermeture, generator, exercise_date_n
    *ptdelta1 = (p1 - *ptprice) / (s1 * increment);
    *ptdelta2 = (p2 - *ptprice) / (s2 * increment);
}
}
return init_mc;
}

int CALC(MC_RandomQuantization2D)(void *Opt, void *Mod, PricingMethod *Met)
{
    TYPEOPT *ptOpt = (TYPEOPT *)Opt;

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    TYPEMOD *ptMod = (TYPEMOD *)Mod;
    double r, divid1, divid2;

    r = log(1. + ptMod->R.Val.V_DOUBLE / 100.);
    divid1 = log(1. + ptMod->Divid1.Val.V_DOUBLE / 100.);
    divid2 = log(1. + ptMod->Divid2.Val.V_DOUBLE / 100.);

    return MCRandomQuantization2D(ptMod->S01.Val.V_PDOUBLE,
                                   ptMod->S02.Val.V_PDOUBLE,
                                   ptOpt->PayOff.Val.V_NUMFUNC_2,
                                   ptOpt->Maturity.Val.V_DATE - ptMod->T.Val.V_DATE,
                                   r,
                                   divid1,
                                   divid2,
                                   ptMod->Sigma1.Val.V_PDOUBLE,
                                   ptMod->Sigma2.Val.V_PDOUBLE,
                                   ptMod->Rho.Val.V_RGDOUBLE,
                                   Met->Par[0].Val.V_LONG,
                                   Met->Par[1].Val.V_ENUM.value,
                                   Met->Par[2].Val.V_PDOUBLE,
                                   Met->Par[3].Val.V_INT,
                                   Met->Par[4].Val.V_INT,
                                   &(Met->Res[0].Val.V_DOUBLE),
                                   &(Met->Res[1].Val.V_DOUBLE), &(Met->Res[2].Val.V_DOUBLE)
    }

static int CHK_OPT(MC_RandomQuantization2D)(void *Opt, void *Mod)
{
    Option *ptOpt = (Option *)Opt;
    TYPEOPT *opt = (TYPEOPT *) (ptOpt->TypeOpt);

    if ((opt->EuOrAm).Val.V_BOOL == AMER)
        return OK;
    else
        return WRONG;
}

static int MET(Init)(PricingMethod *Met, Option *Opt)
{
    if (Met->init == 0)

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{
    Met->init = 1;
    Met->Par[0].Val.V_LONG = 10000;
    Met->Par[1].Val.V_ENUM.value = 0;
    Met->Par[1].Val.V_ENUM.members = &PremiaEnumMCRNGs;
    Met->Par[2].Val.V_PDOUBLE = 0.1;
    Met->Par[3].Val.V_INT = 20;
    Met->Par[4].Val.V_INT = 250;

}
return OK;
}

PricingMethod MET(MC_RandomQuantization2D) =
{
    "MC_RandomQuantization2d",
    { {"N iterations", LONG, {100}, ALLOW},
      {"RandomGenerator", ENUM, {100}, ALLOW},
      {"Delta Increment Rel", PDOUBLE, {100}, ALLOW},
      {"Number of Exercise Dates (0->Geske Johnson Formulae)", INT, {100}, ALLOW},
      {"Tesselation Size", INT, {100}, ALLOW},
      {" ", PREMIA_NULLTYPE, {0}, FORBID}
    },
    CALC(MC_RandomQuantization2D),
    { {"Price", DOUBLE, {100}, FORBID},
      {"Delta1", DOUBLE, {100}, FORBID} ,
      {"Delta2", DOUBLE, {100}, FORBID},
      {" ", PREMIA_NULLTYPE, {0}, FORBID}
    },
    CHK_OPT(MC_RandomQuantization2D),
    CHK_mc,
    MET(Init)
};

```