

## [Help](#)

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#include <stdlib.h>
#include "
href../../mod/doublehes1d/doublehes1d_std/doublehes1d_std_h_src.pdfhes1d_std.
#include "pnl/pnl_matrix.h"
#include "
href../../common/enums_h_src.pdfenums.h"

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion < (2013+2) //The "#els
static int CHK_OPT(MC_TwoLevel_ImportanceSampling)(void *Opt, void *Mod)
{
    return NONACTIVE;
}
int CALC(MC_TwoLevel_ImportanceSampling)(void *Opt, void *Mod, PricingMethod *Me
{
    return AVAILABLE_IN_FULL_PREMIA;
}
#else

/* Calculus of the optimal parameter which minimizes the variance by using the C
static void Simul_theta(int flag_call, int type_generator, int Strike, int step_
{
    int RM = 100000; /* number of iterations of Robbins-Monro algorithm */
    double S_t, g1, g2;
    double h ;
    double sqrt_h , sqrt_rho;
    long i, ii;
    double dot1, a = 1, b = 1, payoffcarre, val_test, temp1, temp2, expo, C = 100;
    double dot2, U_1, U_2, B1_tilde, B2_tilde, B3_tilde, B4_tilde;
    double x_1 = 0.;
    double V_t, NormalValue1, NormalValue2, value, gamma_step;
    PnlVect *m_Mu1, *m_Mu2;

    h = T / step_number; /* discretization step */
    sqrt_h = sqrt(h);
    sqrt_rho = sqrt(1. - SQR(rho));
    m_Mu1 = pnl_vect_create_from_double(RM + 1, 0);
    m_Mu2 = pnl_vect_create_from_double(RM + 1, 0);
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/* Initialisation du générateur */
pnl_rand_init(type_generator, step_number, 2 * step_number);

*theta1 = 0;
*theta2 = 0;

for (ii = 0; ii < RM; ii++)
{
    S_t = s; /* Spot initialisation */
    V_t = sigma0; /* Variance initialisation */
    NormalValue1 = 0.0;
    NormalValue2 = 0.0;
    U_1 = 0.;
    U_2 = 0.;
    B1_tilde = pnl_rand_normal(type_generator);
    B2_tilde = pnl_rand_normal(type_generator);
    B3_tilde = pnl_rand_normal(type_generator);
    B4_tilde = pnl_rand_normal(type_generator);
    for (i = 0 ; i < step_number ; i++)
    {
        g1 = pnl_rand_normal(type_generator);
        NormalValue1 += g1;
        S_t *= (1 + (r - divid) * h + sqrt(V_t) * sqrt_h * g1); /* Price simul
        g2 = pnl_rand_normal(type_generator);
        NormalValue2 += g2;
        value = rho * g1 + sqrt_rho * g2;
        V_t = V_t + k * (theta - V_t) * h + sigma2 * sqrt_h * sqrt(V_t) * valu
        V_t = fabs(V_t); /* Absolute value of V */
    }

    U_1 = U_1 * (1 + r * h) + sqrt(V_t) * (U_1 * sqrt_h * NormalValue1 - sqrt(
    U_2 = U_2 * (1 - k * h) + ((rho * sigma2) / (2 * sqrt(V_t))) * (U_2 * sqrt

    dot2 = GET(m_Mu1, ii) * GET(m_Mu1, ii) + GET(m_Mu2, ii) * GET(m_Mu2, ii);
    dot1 = sqrt_h * NormalValue1 * GET(m_Mu1, ii) + sqrt_h * NormalValue2 * GE
    if (flag_call == 1)
        payoffcarre = SQR(MAX(S_t - Strike, 0)) + SQR(PNL_SIGN(Strike - S_t) * U
    else
        payoffcarre = SQR(MAX(Strike - S_t, 0)) + SQR(PNL_SIGN(S_t - Strike) * U
    expo = exp(-dot1 + 0.5 * dot2 * T);

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temp1 = (GET(m_Mu1, ii) - sqrt_h * NormalValue1) * expo * payoffcarre;
temp2 = (GET(m_Mu2, ii) - sqrt_h * NormalValue2) * expo * payoffcarre;

gamma_step = a / (b + ii);
val_test = SQR(GET(m_Mu1, ii) - gamma_step * temp1) + SQR(GET(m_Mu2, ii) -
val_test = sqrt(val_test);
/* if the (n+1)th estimator of theta is into the compact C*/
if (val_test < C)
{
    LET(m_Mu1, ii + 1) = GET(m_Mu1, ii) - gamma_step * temp1;
    LET(m_Mu2, ii + 1) = GET(m_Mu2, ii) - gamma_step * temp2;
}
/* else reinitialize theta */
else
{
    LET(m_Mu1, ii + 1) = x_1;
    LET(m_Mu2, ii + 1) = x_1;
    C += 1;
}

}

*theta1 = GET(m_Mu1, RM);
*theta2 = GET(m_Mu2, RM);

pnl_vect_free(&m_Mu1);
pnl_vect_free(&m_Mu2);

return;
}

static int MCTwoLevel_ImportanceSampling(double s, NumFunc_1 *p, double T, double
{
    long i, imc, j;
    double price_sample, mean_price, var_price, price_sample1, mean_price1, var_price1;
    double mean_delta, delta_sample, delta_sample1, delta_sample2, mean_delta1, var_delta1;
    double dot1 = 0., dot2 = 0.;
    double S_t, S1_t, S2_t, g1, g2;
    long nb_MC, nb_MC_1;
    int m;
    double h, H;

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double ptprice1, ptprice2, pterror_price1, pterror_price2;
double sqrt_h , sqrt_H, sqrt_rho;
int step_number;
double V_t, V1_t, V2_t, value, NormalValue1, NormalValue2;
double theta1, theta2;
PnlVect *B1, *B2;

double Strike;
double alpha, z_alpha;
double pterror_price;
int flag_call;

if ((p->Compute) == &Call)
    flag_call = 1;
else
    flag_call = 0;

Strike = p->Par[0].Val.V_PDOUBLE;

/* Value to construct the confidence interval */
alpha = (1. - confidence) / 2.;
z_alpha = pnl_inv_cdfnor(1. - alpha);

m = (int)(sqrt(n));
step_number = m;
nb_MC = pow(m, 4.);
nb_MC_1 = CUB(m);
h = T / (SQR(m)); /* fine step of discretization */
H = T / m; /* coarse step of discretization */
sqrt_h = sqrt(h);
sqrt_H = sqrt(H);
sqrt_rho = sqrt(1. - SQR(rho));
B1 = pnl_vect_create_from_double(SQR(step_number) + 1, 0);
B2 = pnl_vect_create_from_double(SQR(step_number) + 1, 0);

/*Initialisation*/
mean_price = 0.;
var_price = 0.;
mean_delta = 0.;
var_delta = 0.;

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/* Calculus of the optimal theta */
Simul_theta(flag_call, generator, Strike, 100, T, s, r, divid, V0, k, theta, s

dot2 = SQR(theta1) + SQR(theta2);
/* First Monte Carlo Sampling nb_MC=(n^2) */
for (imc = 1; imc <= nb_MC; imc++)
{
    /* Begin of the nb_MC iterations */
    S_t = s;
    V_t = V0;
    NormalValue1 = 0.;
    NormalValue2 = 0.;
    /* Discretization using the coarse step*/
    for (i = 0 ; i < step_number ; i++)
    {
        g1 = pnl_rand_normal(generator);
        NormalValue1 += g1;
        S_t = S_t * (1 + (r - divid) * H + sqrt(V_t) * sqrt_H * (g1 + sqrt_H *
        g2 = pnl_rand_normal(generator);
        NormalValue2 += g2;
        value = rho * (g1 + sqrt_H * theta1) + sqrt_rho * (g2 + sqrt_H * theta
        V_t = V_t + k * (theta - V_t) * H + sigma2 * sqrt_H * sqrt(V_t) * valu
        V_t = fabs(V_t);
    }

dot1 = theta1 * sqrt_H * NormalValue1 + theta2 * sqrt_H * NormalValue2;
/*Call Price*/
if (flag_call == 1)
{
    price_sample= exp(-r * T) * MAX(S_t - Strike, 0) * exp(-dot1 - 0.5 *
    if (S_t - Strike > 0.0)
        delta_sample = exp(-r * T) * (S_t / s) * exp(-dot1 - 0.5 * dot2 * T)
    else delta_sample = 0.;
}
else //Put Price
{
    price_sample = exp(-r * T) * MAX(Strike - S_t, 0) * exp(-dot1 - 0.5 *
    if (Strike - S_t > 0.0)
        delta_sample = exp(-r * T) * (-S_t / s) * exp(-dot1 - 0.5 * dot2 * T

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        else delta_sample = 0.;
    }

    /* mean */
    mean_price += price_sample / nb_MC;
    mean_delta += delta_sample / nb_MC;

    /* Variance */
    var_price += SQR(price_sample - mean_price) / nb_MC;
    var_delta += SQR(delta_sample - mean_delta) / nb_MC;
}

/* End of the nb_MC iterations */

mean_price1 = 0.;
var_price1 = 0.;
mean_delta1 = 0.;
var_delta1 = 0.;

/*Second Monte Carlo sampling (nb_MC_1=n^(3/2))*/
for (imc = 1; imc <= nb_MC_1; imc++)
{
    /* Begin of the nb_MC_1 iterations */
    S1_t = s;
    S2_t = s;
    V1_t = V0;
    V2_t = V0;
    /* Discretization using the fine step */
    for (i = 0 ; i < SQR(step_number) ; i++)
    {
        g1 = pnl_rand_normal(generator);
        LET(B1, i + 1) = GET(B1, i) + sqrt_h * g1;
        S1_t = S1_t * (1 + (r - divid) * h + sqrt(V1_t) * ((GET(B1, i + 1) - G
        g2 = pnl_rand_normal(generator);
        LET(B2, i + 1) = GET(B2, i) + sqrt_h * g2;
        value = rho * ((GET(B1, i + 1) - GET(B1, i)) + h * theta1) + sqrt_rho
        V1_t = V1_t + k * (theta - V1_t) * h + sigma2 * sqrt(V1_t) * value;
        V1_t = fabs(V1_t);
    }

    /* Discretization using the coarse step */
    for (j = 0 ; j < step_number ; j++)

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    {
        S2_t = S2_t * (1 + (r - divid) * H + sqrt(V2_t) * ((GET(B1, step_number *
        value = rho * ((GET(B1, step_number * (j + 1)) - GET(B1, step_number *
        V2_t = V2_t + k * (theta - V2_t) * H + sigma2 * sqrt(V2_t) * value;
        V2_t = fabs(V2_t);
    }
    dot1 = theta1 * GET(B1, SQR(step_number)) + theta2 * GET(B2, SQR(step_number));
    /* Call price of the difference */
    if (flag_call == 1)
    {
        price_sample1 = exp(-r * T) * (MAX(S1_t - Strike, 0) - MAX(S2_t - Strike, 0));
        /*Delta Call 1*/
        if (S1_t - Strike > 0.0)
            delta_sample1 = exp(-r * T) * (S1_t / s) * exp(-dot1 - 0.5 * dot2 *
        else delta_sample1 = 0.;
        /*Delta Call 2*/
        if (S2_t - Strike > 0.0)
            delta_sample2 = exp(-r * T) * (S2_t / s) * exp(-dot1 - 0.5 * dot2 *
        else delta_sample2 = 0.;
    }
    else//Put Case
    {
        price_sample1 = exp(-r * T) * (MAX(-S1_t + Strike, 0) - MAX(-S2_t + Strike, 0));
        /*Delta Put 1*/
        if (Strike - S1_t > 0.0)
            delta_sample1 = exp(-r * T) * (-S1_t / s) * exp(-dot1 - 0.5 * dot2 *
        else delta_sample1 = 0.;
        /*Delta Put 2*/
        if (Strike - S2_t > 0.0)
            delta_sample2 = exp(-r * T) * (-S2_t / s) * exp(-dot1 - 0.5 * dot2 *
        else delta_sample2 = 0.;
    }
    /* mean */
    mean_price1 += price_sample1 / nb_MC_1;
    mean_delta1 += (delta_sample1 - delta_sample2) / nb_MC_1;

    /* variance */
    var_price1 += SQR(price_sample1 - mean_price1) / nb_MC_1;
    var_delta1 += SQR(delta_sample1 - delta_sample2 - mean_delta1) / nb_MC_1;
}
/* End of the nb_MC_1 iterations */

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/* Statistical Romberg Price */
ptprice1 = mean_price;
pterror_price1 = sqrt(var_price) / (sqrt(nb_MC) - 1);
ptprice2 = mean_price1;
pterror_price2 = sqrt(var_price1) / (sqrt(nb_MC) - 1);

*ptprice = ((ptprice1) + (ptprice2)); /* European price using the Statistical
pterror_price = pterror_price1 + pterror_price2; /* Length of 95% confidence i

/* Price Confidence Interval */
*inf_price = *ptprice - z_alpha * pterror_price;
*sup_price = *ptprice + z_alpha * pterror_price;

/* Delta estimator */
ptdelta = mean_delta;
pterror_delta = sqrt(var_delta) / (sqrt(nb_MC) - 1);
ptdelta1 = mean_delta1;
pterror_delta1 = sqrt(var_delta1) / (sqrt(nb_MC) - 1);
*ptdelta2 = ptdelta + ptdelta1;
pterror_delta2 = pterror_delta + pterror_delta1;

/* Delta Confidence Interval */
*inf_delta = *ptdelta2 - 1.96 * (pterror_delta2);
*sup_delta = *ptdelta2 + 1.96 * (pterror_delta2);

pnl_vect_free(&B1);
pnl_vect_free(&B2);

return OK;
}

int CALC(MC_TwoLevel_ImportanceSampling)(void *Opt, void *Mod, PricingMethod *Me
{
    TYPEOPT *ptOpt = (TYPEOPT *)Opt;
    TYPEMOD *ptMod = (TYPEMOD *)Mod;
    double r, divid;

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r = log(1. + ptMod->R.Val.V_DOUBLE / 100.);
divid = log(1. + ptMod->Divid.Val.V_DOUBLE / 100.);

return MCTwoLevel_ImportanceSampling(ptMod->S0.Val.V_PDOUBLE,
                                     ptOpt->PayOff.Val.V_NUMFUNC_1,
                                     ptOpt->Maturity.Val.V_DATE - ptMod->T.Val
                                     r,
                                     divid, ptMod->Sigma0.Val.V_PDOUBLE
                                     , ptMod->MeanReversion.Val.V_PDOUBLE,
                                     ptMod->LongRunVariance.Val.V_PDOUBLE,
                                     ptMod->Sigma.Val.V_PDOUBLE,
                                     ptMod->Rho.Val.V_PDOUBLE,
                                     Met->Par[0].Val.V_INT,
                                     Met->Par[1].Val.V_ENUM.value,
                                     Met->Par[2].Val.V_PDOUBLE,
                                     &(Met->Res[0].Val.V_DOUBLE),
                                     &(Met->Res[1].Val.V_DOUBLE),
                                     &(Met->Res[2].Val.V_DOUBLE),
                                     &(Met->Res[3].Val.V_DOUBLE),
                                     &(Met->Res[4].Val.V_DOUBLE),
                                     &(Met->Res[5].Val.V_DOUBLE)
                                     );
}

static int CHK_OPT(MC_TwoLevel_ImportanceSampling)(void *Opt, void *Mod)
{
    if ((strcmp(((Option *)Opt)->Name, "CallEuro") == 0) || (strcmp(((Option *)Opt
        return OK;

    return WRONG;
}

#endif //PremiaCurrentVersion

static int MET(Init)(PricingMethod *Met, Option *Opt)
{
    if (Met->init == 0)
    {

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    Met->init = 1;

    Met->Par[0].Val.V_INT = 400;
    Met->Par[1].Val.V_ENUM.value = 0;
    Met->Par[1].Val.V_ENUM.members = &PremiaEnumRNGs;
    Met->Par[2].Val.V_DOUBLE = 0.95;
}
return OK;
}

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PricingMethod MET(MC_TwoLevel_ImportanceSampling) =
{
    "MC_TwoLevel_ImportanceSampling",
    {
        {"TimeStepNumber", LONG, {100}, ALLOW},
        {"RandomGenerator", ENUM, {100}, ALLOW},
        {"Confidence Value", DOUBLE, {100}, ALLOW},
        {" ", PREMIA_NULLTYPE, {0}, FORBID}
    },
    CALC(MC_TwoLevel_ImportanceSampling),
    { {"Price", DOUBLE, {100}, FORBID},
      {"Delta", DOUBLE, {100}, FORBID} ,
      {"Inf Price", DOUBLE, {100}, FORBID},
      {"Sup Price", DOUBLE, {100}, FORBID} ,
      {"Inf Delta", DOUBLE, {100}, FORBID},
      {"Sup Delta", DOUBLE, {100}, FORBID} ,
      {" ", PREMIA_NULLTYPE, {0}, FORBID}
    },
    CHK_OPT(MC_TwoLevel_ImportanceSampling),
    CHK_mc,
    MET(Init)
};

```