

[Help](#)

```
#if defined(PremiaCurrentVersion) && PremiaCurrentVersion < (2008+2) //The "#els
#else

#include <
href../../../../common/math/cdo/cdo_math_h_src.pdfmath.h>
#include <stdio.h>
#include <stdlib.h>

/* To evaluate the cubic spline interpolant at a specified point

XB : (input) point at which interpolation is required
N : (input) Number of points in the table
X : (input) Array of length N, containing the abscissas
F : (input) Array of length N, containing the function values at X[I]
C : (input) Array of length 3*N containing the spline coefficients
which should have been calculated using SPLINE
DFB : (output) First derivative of spline at x=XB
DDFB : (output) Second derivative of spline at x=XB
IER : (output) error parameter, IER=0 if execution is successful
IER=24 implies XB is outside the range of table on higher side
IER=25 implies XB is outside the range of table on lower side
IER=201 implies N<2
SPLEVL will be the interpolated value at x=XB

Required functions : None
*/

double splevl(double xb, long n, double x[], double f[], double **c,
              double *dfb, double *ddfb, int *ier)

{
    long igh, nigh, mid;
    double r1, dx;
    static long low = -1;

    if (n < 2)
    {
        *ier = 201;
        return 0.0;
    }
}
```

```

    }

    *ier = 0;
    /* If the previous value of LOW is inadmissible, set the range to (0,N-1) */
    if (low < 0 || low >= n - 1)
    {
        low = 0;
        igh = n - 1;
    }
    else igh = low + 1;

    while ((xb < x[low] && xb < x[igh]) || (xb > x[low] && xb > x[igh]))
    {
        /* Extend the range */
        if ((xb > x[low]) == (x[n - 1] > x[0]))
        {
            /* Extend the range on higher side */
            if (igh >= n - 1)
            {
                *ier = 24;
                low = n - 2;
                break;
            }
            else
            {
                nigh = igh + 2 * (igh - low);
                if (n - 1 < nigh) nigh = n - 1;
                low = igh;
                igh = nigh;
            }
        }

        else
        {
            /* Extend the range on lower side */
            if (low <= 0)
            {
                *ier = 25;
                igh = low + 1;
                break;
            }
        }
    }

```

```

        else
        {
            nigh = low;
            low = low - 2 * (igh - low);
            if (low < 0) low = 0;
            igh = nigh;
        }
    }
}

/* Once the point is bracketed between two tabular points locate it by bisection
while ((igh - low > 1) && (xb != x[low]))
{
    mid = (low + igh) / 2;
    if ((xb <= x[mid]) == (xb <= x[low])) low = mid;
    else igh = mid;
}

dx = xb - x[low];
r1 = ((c[low][2] * dx + c[low][1]) * dx + c[low][0]) * dx + f[low];
*dffb = (3.0 * c[low][2] * dx + 2.*c[low][1]) * dx + c[low][0];
*ddffb = 6.*c[low][2] * dx + 2.*c[low][1];
return r1;
}

/* To calculate coefficients of cubic spline interpolation with
not-a-knot boundary conditions

X : (input) Array of length N containing x values
F : (input) Array of length N containing values of function at X[I]
F[I] is the tabulated function value at X[I].
N : (input) Length of table X, F
C : (output) Array of length 3*N containing the spline coefficients

Error status is returned by the value of the function SPLINE.
0 value implies successful execution
201 implies that N<2

```

Required functions : None

*/

```
int spline(double x[], double f[], long n, double **c)

{
    long i, j;
    double g, c1, cn, div12, div01;

    if (n < 2) return 201;
    else if (n == 2)
    {
        /* Use linear interpolation */
        c[0][0] = (f[1] - f[0]) / (x[1] - x[0]);
        c[0][1] = 0.0;
        c[0][2] = 0.0;
        return 0;
    }
    else if (n == 3)
    {
        /* Use quadratic interpolation */
        div01 = (f[1] - f[0]) / (x[1] - x[0]);
        div12 = (f[2] - f[1]) / (x[2] - x[1]);
        c[0][2] = 0.0;
        c[1][2] = 0.0;
        c[0][1] = (div12 - div01) / (x[2] - x[0]);
        c[1][1] = c[0][1];
        c[0][0] = div01 + c[0][1] * (x[0] - x[1]);
        c[1][0] = div12 + c[0][1] * (x[1] - x[2]);
        return 0;
    }
    else
    {
        /* Use cubic splines

        Setting up the coefficients of tridiagonal matrix */
        c[n - 1][2] = (f[n - 1] - f[n - 2]) / (x[n - 1] - x[n - 2]);
        for (i = n - 2; i >= 1; --i)
        {
            c[i][2] = (f[i] - f[i - 1]) / (x[i] - x[i - 1]);
```

```

        c[i][1] = 2.*(x[i + 1] - x[i - 1]);
        /* The right hand sides */
        c[i][0] = 3.*(c[i][2] * (x[i + 1] - x[i]) + c[i + 1][2] * (x[i] - x[i + 1])) / c[i][1];
    }

/* The not-a-knot boundary conditions */
c1 = x[2] - x[0];
c[0][1] = x[2] - x[1];
c[0][0] = c[1][2] * c[0][1] * (2.*c1 + x[1] - x[0]) + c[2][2] * (x[1] - x[0]) * c1;
c[0][0] = c[0][0] / c1;
cn = x[n - 1] - x[n - 3];
c[n - 1][1] = x[n - 2] - x[n - 3];
c[n - 1][0] = c[n - 1][2] * c[n - 1][1] * (2.*cn + x[n - 1] - x[n - 2]) + c[n][2] * (x[n - 1] - x[n - 2]) * cn;
c[n - 1][0] = (c[n - 1][0] + c[n - 2][2] * (x[n - 1] - x[n - 2]) * (x[n - 1] - x[n - 2])) / c[n - 1][1];
/* Solving the equation by Gaussian elimination */
g = (x[2] - x[1]) / c[0][1];
c[1][1] = c[1][1] - g * c1;
c[1][0] = c[1][0] - g * c[0][0];
for (j = 1; j < n - 2; ++j)
{
    g = (x[j + 2] - x[j + 1]) / c[j][1];
    c[j + 1][1] = c[j + 1][1] - g * (x[j] - x[j - 1]);
    c[j + 1][0] = c[j + 1][0] - g * c[j][0];
}
g = cn / c[n - 2][1];
c[n - 1][1] = c[n - 1][1] - g * (x[n - 2] - x[n - 3]);
c[n - 1][0] = c[n - 1][0] - g * c[n - 2][0];

/* The back-substitution */
c[n - 1][0] = c[n - 1][0] / c[n - 1][1];
for (i = n - 2; i >= 1; --i) c[i][0] = (c[i][0] - c[i + 1][0] * (x[i] - x[i + 1])) / c[i][1];
c[0][0] = (c[0][0] - c[1][0] * c1) / c[0][1];

/* Calculating the coefficients of cubic spline */
for (i = 0; i < n - 1; ++i)
{
    c[i][1] = (3.*c[i + 1][2] - 2.*c[i][0] - c[i + 1][0]) / (x[i + 1] - x[i]);
    c[i][2] = (c[i][0] + c[i + 1][0] - 2.*c[i + 1][2]) / ((x[i + 1] - x[i]) * 2);
}
/* Set the coefficients for interval beyond X(N) using continuity

```

```

        of second derivative, although they may not be used. */
        c[n - 1][1] = c[n - 1][1] + 3 * (x[n - 1] - x[n - 2]) * c[n - 2][2];
        c[n - 1][2] = 0.0;
        return 0;
    }
}

```

/* To draw a smooth curve passing through a set of data points
using cubic spline interpolation

NTAB : (input) Number of points in the table
X : (input) Array of length NTAB containing X values
F : (input) Array of length NTAB containing function values at X[I]
C : (output) Array of length 3*NTAB which will contain the spline coefficients
NP : (input) Number of points at which interpolation is to be calculated
XP : (output) Array of length NP containing the x values at
 NP uniformly spaced points for use in plotting
FP : (output) Array of length NP containing interpolated
function values at XP[I]

Error status is returned by the value of the function SMOOTH.
0 value implies successful execution
202 implies NP<=1
other values may be set by SPLINE

Arrays XP and FP can be used to draw a smooth curve through the
tabulated points.

Required functions : SPLINE, SPLEVL
*/

```

int smooth(long ntab, double x[], double f[], double **c, int np, double xp[], d
{
    int i, ier;
    double dx, dfb, ddfb;

    i = spline(x, f, ntab, c);
    if (i > 100) return i;

```

```

    if (np <= 1) return 202;

    dx = (x[ntab - 1] - x[0]) / (np - 1);
    for (i = 0; i < np; ++i)
    {
        xp[i] = x[0] + dx * i;
        fp[i] = splevl(xp[i], ntab, x, f, c, &dfb, &ddfb, &ier);
    }
    return 0;
}

int smoothmod(long ntab, double x[], double f[], double **c, int np, double xp[])
{
    int i, ier;
    double dfb, ddfb;

    i = spline(x, f, ntab, c);
    if (i > 100) return i;

    if (np <= 1) return 202;

    //dx=(x[ntab-1]-x[0])/(np-1);
    for (i = 0; i < np; ++i)
    {
        // xp[i]=x[0]+dx*i;
        fp[i] = splevl(xp[i], ntab, x, f, c, &dfb, &ddfb, &ier);
    }
    return 0;
}

double smoothscalar(long ntab, double x[], double f[], double **c, double xp)
{
    int i, ier ;
    double fp, dfb, ddfb;

    i = spline(x, f, ntab, c);
    if (i > 100) return i;

    fp = splevl(xp, ntab, x, f, c, &dfb, &ddfb, &ier);

```

```
    return fp;
}

#endif //PremiaCurrentVersion
```